Double-Rydberg Molecular Anions

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I. Introduction

A. The Nature of Double-Rydberg Electronic States

Studies of families of unusual species such as the double-Rydberg (DR) anions discussed in this review are of fundamental importance. These investigations expand our knowledge base and understanding of electronic structure and electronic dynamics. As science enters the 1990's, the search for new materials, new reaction pathways, and the design of materials with specified physical and chemical properties will require chemists to extend their conceptual understanding of chemical bonding and electronic structure and their relation to macroscopic behavior. It is the belief of the authors that any and all experience in which novel bonding situations or unusual electronic structures are encountered can contribute to the broadening of chemists' conceptual base. The class of anions treated here are unusual because (i) they are local minima on respective ground-state potential energy hypersurfaces where much more stable global minima exist, so rearrangement of the DR species via barrier tunneling is possible, (ii) they are electronically stable only because the motions of the outermost pair of electrons (i.e., those that occupy the diffuse Rydberg-like orbitals) involve highly radially and angularly correlated motions (i.e., their electronic structures can not be viewed in the conventional "electron pair occupying an orbital" picture), (iii) they possess a multitude of excited electronic



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states that are metastable with respect to electron autodetachment but which may be long lived and hence experimentally accessible.

Each member of the so-called family of double-Rydberg anions¹ consists of an underlying geometrically and electronically stable cation core (referred to as the parent cation) around which a pair of electrons move in diffuse orbitals. Examples of parents that have been studied experimentally or theoretically include the closed-shell 10-electron species Na⁺, NH₄⁺, H₃O⁺, CH₅⁺, Na⁺, H_2F^+ , and NeH⁺, as well as two-electron cations such as H_3^+ and Li⁺. The H⁻ species, whose parent is the "zero-electron" H⁺ has also been characterized. In such studies, it has been of interest to compare the pattern of electronic energy levels observed for isoelectronic systems to determine, for example, if one can analyze these patterns in terms of "crystal field" like splittings of the spherically symmetric case (i.e., can the levels for NH₄ be determined as T_d derivatives of those for Na⁻?). As discussed later in this review, such a model has indeed been successful for the 10-electron DR species.

When might one expect to encounter such DR species? If the cation parent of a DR anion is, at its equilibrium geometry, a closed-shell species such as those mentioned above, the lowest energy states of both the neutral species formed when a single electron moves in a diffuse orbital around the underlying cation core and of the corresponding DR anion involve, in the neighborhood of the parent cation's equilibrium geometry, Rydberg-like rather than valence-like electronic structures. That is, if the parent has no unfilled valence orbitals at its equilibrium geometry, both the neutral and anion must utilize Rydberg orbitals at this geometry.

In contrast, if the parent cation is valence "unsaturated" at its most stable geometry, its neutral daughter and anion may have both stable valence-type electronic states as well as Rydberg-like states. For example, Cl⁺ certainly forms stable valence Cl and Cl-states. In addition, both the neutral (1s²2s²2p⁶3s²3p⁴4s¹) Cl and anion (1s²2s²2p⁶3s²3p⁴4p²) Cl⁻ states exist and consist, respectively, of a 1s²2s²2p⁶3s²3p⁴ cation core with one 4s or a pair of 4p Rydberg-like orbitals (i.e., orbitals one or more quantum number higher than that of the outer valence orbitals). Of course, in these cases for which the parent cation possesses unfilled valence orbitals, the DR anion states will not be the lowest energy states.

B. The Global Geometrical or Thermodynamic Stability of Rydberg and Double-Rydberg States

The Rydberg states of the neutral and of the DR species may or may not be stable with respect to distortion or fragmentation of the underlying nuclear framework. Global stability depends on the strengths of the bonds in the cation and the products of fragmentation as well as the ionization potentials (IPs) and electron affinities (EAs) of these products. For example, the stability of neutral NeH is, as shown in Figure 1, determined by the IP of the Rydberg NeH, the Ne-H bond strength in NeH⁺, and the IP of H. Likewise, the stability of NeH⁻, as shown in Figure 2, is governed by the IP of the DR NeH⁻, the D_e of NeH, and the EA of H.

It should therefore be clear that the Rydberg states of the neutral are unlikely to be thermodynamically stable² unless the bond strength in the parent cation

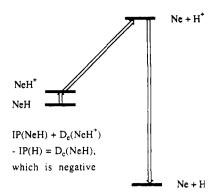


Figure 1. Relative energies of NeH, NeH+, Ne + H, and Ne + H+.

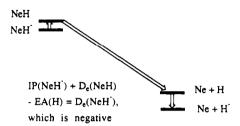


Figure 2. Relative energies of NeH, DR NeH-, Ne + H, and Ne + H⁺.

(NeH⁺ here) is larger than the lowest IP of the fragment species (H atom here). Moreover, the DR anion will probably not be thermodynamically stable unless the neutral Rydberg is, because the IP of the DR state is not likely to exceed that of the fragment (H here).

In addition to the (probable) thermodynamic instability of the Rydberg and DR states, it is important to emphasize that there exist geometries of even lower energy than the fragment species. For example, the lowest energy geometry of NeH corresponds to an Hion bound to a Ne atom through van der Waals attraction; this complex has lower total energy than the separated Ne + H. Likewise, the neutral NeH may exist as a van der Waals New H complex if the zeropoint vibrational energy of the complex does not exceed the depth of the attractive van der Waals potential.

C. Local Geometrical Stability of Rydberg and Double-Rydberg States

In contrast, local geometrical stability for the neutral or the anion (i.e., the shape of the electronic energy surface in the neighborhood of the parent cation's geometry) depends on the forces that the outer electron(s) exert on the underlying core. These forces are partially governed by the symmetry of the occupied Rydberg orbitals of the neutral or anion. State degeneracies arising from Rydberg orbital degeneracies give rise to local Jahn-Teller instability. Crossings of electronic configurations, as shown in Figures 3 and 4, strongly affect the local curvatures and barrier heights and thicknesses on the neutral and anion energy surfaces. Rydberg and DR species can be stable or metastable with respect to tunneling through the barrier if such a barrier exists and is sufficiently "high" and "thick".

In Figure 3, the dominant electronic configuration of the NeH contains two electrons in a bonding $(2p_{\sigma} + 1s_{\sigma})$ orbital connecting the Ne and H atoms and thus forming NeH⁺ plus a single electron in a Rydberg orbital

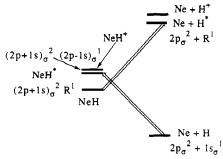


Figure 3. Configuration correlation diagram for NeH and Ne + H.

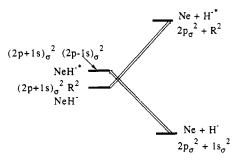


Figure 4. Configuration correlation diagram for DR NeH $^-$ and Ne + H $^-$.

denoted R. In contrast, the lowest electronic state of the fragmentation products Ne + H has all three of these electrons in valence orbitals (two in the $2p_{\sigma}$ on Ne and one in the 1s on H). The $(2p_{\sigma} + 1s_{\sigma})^2R^1$ configuration that dominates the Rydberg NeH correlates with an excited Rydberg state of the products Ne $(2p_{\sigma}^2)$ + H*(R). The $2p_{\sigma}^21s_{\sigma}^1$ configuration that dominates Ne + H correlates with a $\sigma^2\sigma^*$ configuration $(2p_{\sigma} + 1s_{\sigma})^2(2p_{\sigma} - 1s_{\sigma})$ of NeH.

The avoided crossing between the two configurations depicted in Figure 3 may, depending on the extent to which the two configurations are coupled, produce a barrier on the NeH \Rightarrow Ne + H energy surface. Because the two configurations differ by a single spin-orbital occupancy (i.e., the R orbital in one configuration occurs where the σ^* orbital appears in the second configuration), it would be expected³ that this configuration crossing would be "strongly avoided", and thus that the barrier on the surface would either be low or nonexistent.

In Figure 4, the dominant electronic configuration of the DR NeH⁻ contains two electrons in a bonding $(2p_{\sigma} + 1s_{\sigma})$ orbital between the Ne and H atoms plus two Rydberg electrons, denoted R² (these two electrons need not be in the same Rydberg orbital; the notation R² is used simply to indicate that there are two electrons that occupy nonvalence orbitals). In contrast, the lowest electronic state of the fragmentation products Ne + H-has all of these electrons in valence orbitals (two in the $2p_{\sigma}$ on Ne and two in the valence orbitals on H). The $(2p_{\sigma} + 1s_{\sigma})^2R^2$ configuration that dominates NeH-correlates with an excited Rydberg state of the products Ne $(2p_{\sigma}^2) + H^{-*}(R^2)$. The $2p_{\sigma}^2 1s_{\sigma}^2$ configuration that dominates Ne + H- correlates with a $\sigma^2\sigma^{*2}$ configuration $(2p_{\sigma} + 1s_{\sigma})^2(2p_{\sigma} - 1s_{\sigma})^2$ of NeH-.

The avoided crossing between these configurations depicted in Figure 4 may, depending on the extent to which the two configurations are coupled, produce a barrier on the NeH⁻ → Ne + H⁻ energy surface. In the

anion case, unlike that of the neutral, the two configurations that cross differ by two spin-orbital occupancies. In this case, only the two-electron part of the electronic hamiltonian can couple these configurations, and such crossings can be expected³ to be "weakly avoided". As a result, the barrier on the anion surface is more likely to be substantial.

The difference in the dominant electronic configurations of the Rydberg neutral species and its fragmentation products as well as the DR anion and its fragments gives rise to the possibility that barriers may exist on the respective electronic energy surfaces. The possibilities are better for the DR anion than for the neutral. If such a barrier exists, the corresponding species may be sufficiently long-lived to be experimentally observed.

D. Electronic Stability and Metastability of Double-Rydberg States

In addition to the possibility of geometrical instability, some states of the DR species may be stable with respect to electron autodetachment and others may be unstable (but perhaps long lived). This depends on the relative energies of the anion and neutral states as functions of geometry. Even if the anion's lowest-energy state lies below the ground state of the neutral at the parent cation geometry (and is therefore locally electronically bound), the ground-state anion surface may "penetrate" the neutral surface at some other geometry, upon which facile electron ejection may occur.

The possibility of electronically metastable DR states has to do with the electronic structure of the specific anion state relative to the electronic structure(s) of neutral-species states that lie energetically below it. For example, the 4s2 1S DR state of Na-lies above the 3s1 ²S and 3p¹ ²P states of neutral Na, so this DR state is not stable⁴ with respect to electron loss. However, because the 4s2 configuration differs from the "detachment-channel" 'S configurations to which the hamiltonian can couple it (i.e., 3s1ks1 and 3p1kp1, where ks and kp denote outgoing continuum orbitals of s- and p-wave symmetry) by two spin-orbital occupancies, the coupling to these detachment channels can be expected to be weak. As a result, the 4s2 state may be rather long-lived and may appear as a "resonance" in spectroscopic or electron-scattering experiments.

E. Summary

DR atomic and molecular anions clearly show potential for displaying novel electronic and geometrical structure characteristics. For each such species, one expects a progression of neutral Rydberg electronic states with energies converging to the energy of the parent cation; some of these Rydberg states may be locally geometrically stable, and others may not.

In the neighborhood of each Rydberg state of the neutral, the possibility of DR states arises. If the neutral Rydberg state has a single electron in an orbital of quantum number n, the DR states that are most likely to arise involve either n^2 or n^1n^4 orbital occupancy, with n' > n. For example, see in Figures 5–7 the rich pattern of neutral and anion states that Schulz reports⁴ for H⁻, Li⁻, and Na⁻.

If the lowest energy DR state lies below the lowest neutral Rydberg state, it is termed "electronically

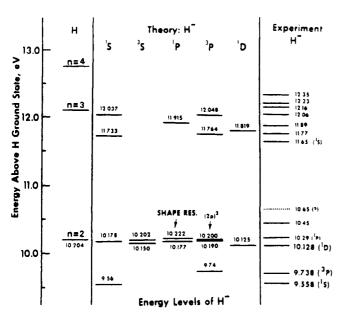


Figure 5. Energy level patterns for H and H- (from ref 4).

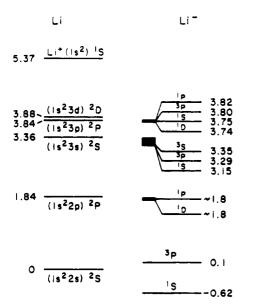


Figure 6. Energy level patterns for Li and Li⁻ (from ref 4).

stable". Excited DR states that lie above neutral Rydberg states whose electronic configurations require a "two-electron" process for electron ejection are termed "Feshbach resonances" (e.g., the $4s^2$ state of Na⁻ discussed above lies below the 4s state of Na but above the 3s and 3p states of Na). Such states may be rather long lived because of the weak coupling that occurs between these two configurations. The higher energy configuration contains two orbitals of principal quantum number n greater than that of the other configuration, which contains one orbital with n' < n and one oscillatory continuum orbital.

DR states that lie above neutral Rydberg states to which they can autoionize via a "one-electron" process can be metastable if the orbital that is involved in the electron ejection possesses angular momentum (i.e., is a p, d, etc. orbital). For example, the 2s¹2p¹ ³P state of Li⁻ is metastable⁴ although it can autoionize to the 2s¹ state of Li by ejecting the 2p electron (but it can not eject the 2s electron to produce the 2p¹ state because its energy is not high enough). Also, the 3s¹3p¹ ³P state

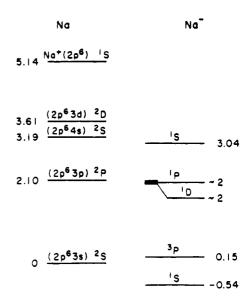


Figure 7. Energy level patterns for Na and Na⁻ (from ref 4).

of Li⁻ is metastable although it lies above the 3s state (but not the 3p state) of Li.

These states are metastable because the electron ejection process requires tunneling of the electron through the centrifugal barrier provided by the I(I+1) $\hbar^2/2m_er^2$ factor in the radial kinetic energy operator. Such metastable states are termed "shape resonances". In the former example, where decay can occur to the ground $2s^1$ state of the neutral species, one says that the $2s^12p^1$ ³P state is a simple shape resonance. In the latter case, where decay can occur to the nearby excited $3s^1$ state of the neutral, one says that the $3s^13p^1$ ³P state is a "core-excited" shape resonance because the neutral is produced in an excited state when the 3p electron is ejected.

In addition to these electronic-state intricacies, the Rydberg and DR species present interesting local and global geometrical-stability issues. Both molecular species are probably not, even in their ground states, thermodynamically stable. However, depending on the nature of the Rydberg and valence orbitals that appear in their electronic configurations, they may be locally stable; the DR anions have better chances for achieving local stability than do the Rydberg neutrals. Local stability, of course, only means that a barrier exists and that this barrier can slow fragmentation, whose rate is determined by the masses of the atoms involved and the height and thickness of the barrier.

II. What is Known about Double-Rydberg Anions?

A. H₃-

The low-energy Rydberg states of neutral H_3 were observed by Herzberg in 1979 in emission spectra⁵ and by Vogler in translation spectra.⁶ This work and subsequent efforts by Garvey and Kuppermann,⁷ Griffiths, Harris, and Benyon,⁸ and by Gellene and Porter⁹ established the lowest electronic state of H_3 at the D_{3h} geometry of the parent cation to be the ²E'(2p) Rydberg state. This state was seen to be Jahn-Teller unstable locally, and, in fact, globally unstable with respect to fragmentation to H_3 . Excited Rydberg states of

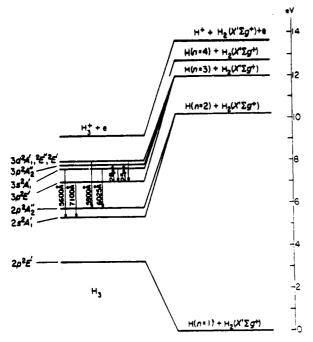


Figure 8. H₃ Rydberg state energy level pattern (from ref 18).

 H_3 having $^2A'_1(2s)$, $^2A''_2(2p)$, $^2E'(3p)$, $^2A'_1(3s)$, $^2A''_2(3p)$, $^2A_1'(3d)$, $^2E''(3d)$, and $^2E'(3d)$ symmetries have also been characterized spectroscopically $^{10-12}$ (see Figure 8).

Theoretical calculations using explicit Rydberg-like basis functions were carried out in 1979 by King and Morokuma, ¹³ by Jungen, ¹⁴ and by Martin. ¹⁵ The results of these calculations were essentially in agreement with what Herzberg⁵ found that same year. Subsequently, Nager and Jungen ¹⁶ examined many more excited states (most of which were not yet observed), Raynor and Herschbach² studied the geometrical stabilities of various Rydberg states of H₃ and of other species, and Petsalakis, Theodorakopoulos, and Wright¹⁷ examined electronic transition moments among several low-energy Rydberg states at various geometries.

To the best of our knowledge, DR ${\rm H_3^-}$ has not been seen experimentally. Its lowest energy state, at the parent cation geometry, might be expected to doubly occupy the e' (2p) orbitals. However, our calculations¹ indicate that the lowest electronic state of DR ${\rm H_3^-}$ has a dominant ${\rm a_1^2}$ (2s²) Rydberg orbital occupancy. We find this ${}^1{\rm A'_1}$ state to be electronically unstable with respect to the dissociative ${}^2{\rm E'}$ state of the neutral; it may be metastable because its 2s² occupancy differs by two orbitals from that of the ${}^2{\rm E'}$ (2p) neutral with an ejected p-wave electron. We also identified¹ excited states of ${\rm H_3^-}$ of ${}^3{\rm A''}_2(2{\rm s2p})$, ${}^1{\rm A'}_1(3{\rm s^2})$, and ${}^3{\rm A''}_2(3{\rm s3p})$ symmetry, each of which lies below the states of the neutral to which it can decay via one-electron processes.

B. NH₄-

The Rydberg neutral species NH_4 has been the subject of several experimental and theoretical studies. In 1981, Herzberg¹⁸ obtained the first experimental evidence for Rydberg states of this species. Gallene, Cleary, and Porter¹⁹ in 1982 used their neutralized ion-beam experimental method to determine that NH_4 has a lifetime, presumably with respect to fragmentation, of less than 1 μ s, while ND_4 has a lifetime in excess of 20 μ s. These data indicate that there is a small

barrier on the NH₄ surface and that the slower tunneling of the D isotope leads to a longer lifetime.

In 1982, Havriliak and King²⁰ studied several Rydberg states of NH₄ using Rayleigh-Schrödinger perturbation theory, focusing on transition moments, force constants, energies, and Jahn-Teller parameters. Raynor and Herschbach,² as part of their systematic study of several Rydberg species, examined several low-lying electronic states of NH₄ in 1982. Havriliak, Furlani, and King²¹ improved on their earlier calculations in 1984, and Cardy, Liotard, Dargelos, Marinelli, and Roche²² examined vibronic coupling effects in the ${}^{2}\mathrm{T}_{2}(3\mathrm{p})$ state in 1988. The thermodynamic and kinetic stabilities of NH4 and its deuterated forms have been studied by McMaster et al.,23 Cardy et al.,24 Kaspar et al.,25 and by Kassab and Evleth.26 The conclusions of these papers concerning the relative energies and stabilities of the Rydberg states are qualitatively similar. The ²A₁(3s) ground state is thermodynamically unstable although there is a substantial barrier along the dissociation path. There are excited ${}^{2}T_{2}(3p)$, ${}^{2}A_{1}(4s)$, and ²T₂(3d) states all of which are spectroscopically im-

The NH₄⁻ DR structure was studied in 1984 by Kalcher, Rosmus, and Quack²⁷ and in 1986 by Cardy, Larrieu, and Dargelos²⁸ as well as Cremer and Kraka.²⁹ These workers did not, to the best of our knowledge, recognize the DR nature of the ground state they examined, and they did not search for excited DR states. They concluded that the ¹A₁(3s²) ground state is thermodynamically unstable (but not by more than a few kcal/mol) and that there is a barrier that makes this state locally stable. The potential energy barrier for the dissociation of NH₄⁻ was found to be higher than that for dissociation of the neutral (18.6 versus 13.8 kcal mol⁻¹)²⁸ in agreement with the avoided configuration crossing arguments discussed earlier in this review (Figures 3 and 4).

In 1987, after the announcement by Bowen and Eaton³⁰ that DR NH₄⁻ had probably been seen in photoelectron spectroscopy experiments, Ortiz³¹ carried out detailed geometry optimization and energy studies of the NH₃ + H⁻, NH₃····H⁻ and DR NH₄⁻ species. The electron-binding energy of 0.42 eV obtained by Ortiz for DR NH₄⁻ is in excellent agreement with the experimental value^{30,32,33} of 0.50 eV.

It was rather surprising to have seen any appreciable amount of the DR structure of NH₄ in the ion sources used by the Bowen group. These workers were interested in studying H^{-} ... $(H_3N)_k$ complexes by using laser photoelectron spectroscopic methods. Their source conditions were designed to produce large amounts of these "solvated" H- species, after which mass spectroscopic tools were used to extract anions of the proper charge-to-mass ratio. At this time, it is not known how any significant amount of the DR structure, which is very thermodynamically unfavored, was formed under these source conditions. In the future, it may be possible, with NH₄⁺ used as a precursor and passing this cation through, for example, Cs vapor, to use double charge exchange methods to produce even larger currents of the DR NH₄ species. This method may also be of great use in the search for other DR anions.

In 1988, the authors, together with Hernandez and Taylor, performed ab initio configuration interaction

TABLE I. Bond Lengths (au) and Local Harmonic Vibrational Frequencies (cm⁻¹) for Tetrahedral Structures of NH₄⁺, NH₄, and NH₄⁻ Resulting from CAS MCSCF Calculations

| | NH ₄ + | NH ₄ | NH ₄ - |
|-------------|-------------------|-----------------|-------------------|
| r (N-H) | 1.937 | 1.960 | 1.964 |
| T2 vib | 1543 | 1439 | 1434 |
| E vib | 1776 | 1700 | 1717 |
| A_1 vib | 3384 | 3108 | 3140 |
| T, vib | 3629 | 3328 | 3276 |

calculations¹ on several DR states of $\mathrm{NH_4}^-$ (as well as $\mathrm{H_3}^-$, $\mathrm{H_3O^-}$, $\mathrm{H_2F^-}$, $\mathrm{CH_5}^-$, and $\mathrm{NeH^-}$). The electron-binding energy obtained there (0.45 eV) is in excellent agreement with that of $\mathrm{Ortiz.^{31}}$ Excited ${}^3\mathrm{T_1(3p^2)}$, ${}^1\mathrm{A_1^-}$ (4s²), ${}^3\mathrm{T_1(4p^2)}$, and ${}^1\mathrm{A_1(5s^2)}$ DR states were identified, each of which lies below neutral $\mathrm{NH_4}$ states to which it might detach via one-electron processes. Thus, these states may be metastable Feshbach resonances.

The ground states of the cation, neutral, and anion have all been found by Gutowski and Simons³⁴ to be locally stable at tetrahedral geometries with NH bond lengths (in atomic units; 1 au = 0.529 Å) of 1.937, 1.960, and 1.964, respectively. The corresponding vibrational frequencies of these species are given in Table I. Clearly, the frequencies do not differ much among the three; there are four easily identified NH stretch frequencies near 3500 cm⁻¹ and four internal bending vibrations near 1600 cm⁻¹ in all cases.

C. H₃O-

Experimental evidence for metastable states of D_3O , but not of H_3O , has been reported by Gellene and Porter from analysis of fast neutral beam scattering profiles and collisional reionization mass spectra. So Raskit and Porter, however, found no evidence of metastable $D_3^{18}O$. Griffiths, Harris, and Beynon in 1987 reported experimental evidence by neutralization-reionization spectroscopy of H_3O radicals with a lifetime of 0.41 μ s. However, from an independent neutralization-reionization experiment, March and Young have concluded that there is insufficient evidence to support the claim the H_3O radical survives for a transit time of 0.41 μ s.

Raynor and Herschbach² predicted the ${}^{2}A_{1}(3s)$ state to be the ground state at the parent cation $(C_{3\nu})$ geometry, and they speculate that this state may be locally geometrically stable. This conjecture has been recently confirmed in highly correlated calculations by Ortiz³⁸ and by Talbi and Saxon.³⁹

In 1982, Paulson and Henchman⁴⁰ reported seeing $\rm H_3O^-$ in a reaction of OH⁻ with $\rm H_2O$. Griffiths and Harris⁴¹ also studied $\rm H_3O^-$ in 1987, but it is not clear whether their experimental source contained any of the DR species. Theoretical investigations of the DR states of this anion include those of Cremer and Kraka²⁹ in 1986, of Gutowski, Simons, Hernandez, and Taylor¹ in 1988, of Ortiz³⁸ in 1989, and of Gutowski and Simons in 1990.³⁴ The Ortiz work³⁸ yields an electron binding energy for the $^1\rm A_1(3s^2)$ DR structure of 0.43 eV, which compares well with that of Gutowski and Simons³⁴ (0.46 eV). Candidates for metastable Feshbach excited states of $^3\rm A_2(3p^2)$, $^1\rm A_1(4s^2)$, and $^3\rm A_2(4p^2)$ symmetry were also identified.¹

The ground states of the cation, neutral, and DR anion have been found by Gutowski and Simons³⁴ to

TABLE II. Bond Lengths (au), Angles (deg), and Local Harmonic Frequencies (cm⁻¹) for the H_2O Cation, Neutral, and DR Anion Obtained in $C_{3\nu}$ CAS MCSCF Calculations

| | H ₃ O ⁺ | H ₃ O | H ₃ O- |
|--------------------|-------------------------------|------------------|-------------------|
| r (O-H) | 1.862 | 1.919 | 1.908 |
| ∠HOH | 110.59 | 105.93 | 107.80 |
| A ₁ vib | 1042 | 1035 | 980 |
| A_1 vib | 3527 | 3004 | 3106 |
| E vib | 1632 | 1629 | 566 |
| E vib | 3630 | 2727 | 3046 |
| | | | |

be locally geometrically stable and to possess the geometries and local harmonic vibrational frequencies detailed in Table II.

As in the NH₄⁻ case discussed above, no major structural changes occur when one or two electrons are added to the H₃O⁺ core. The largest change takes place in the E symmetry OH stretching vibration which changes by 900 cm⁻¹ moving from the cation to the neutral. This trend is not surprising, however, because it is precisely along this asymmetric distortion that the neutral and anion experience barriers due to avoided configuration crossings. In line with this point, it is also not surprising that this vibration occurs at lower frequency in the neutral than in the anion.

D. NeH

In Herzberg's 1987 review of Rydberg molecules, 10 experimental evidence is summarized that indicates that the lowest Rydberg state of NeH, which consists of a NeH⁺ cation surrounded by a single Rydberg electron, is geometrically unstable. Emissions from higher Rydberg states are seen, but they are broadened in a way that is interpreted to indicate dissociative instability of the ground state. Also, recent speculations 2 on the existence of a shallow potential well and a dissociation barrier for NeH were proven to be wrong. 43,44

The 1982 calculations of Raynor and Herschbach,² those of Theodorakopoulos, Petsalakis and Buenker⁴⁵ in 1987, and those of Gutowski, Simons, Hernandez, and Taylor¹ and Gutowski and Simons³⁴ indicate that the lowest Rydberg state of NeH is of ²Σ character and that this state does not possess a barrier of sufficient strength to prohibit dissociation. Thus, the ground Rydberg state of NeH is most probably unstable geometrically. All three of these theoretical studies found excited states of ²Π and ²Σ symmetry; Raynor and Herschbach² examined electric dipole transition moments among several such states.

A DR state of the NeH⁻ anion has not been seen experimentally. The 1988 calculations of Gutowski, Simons, Hernandez, and Taylor¹ predict that a DR NeH⁻ state of $^{1}\Sigma$ symmetry should be electronically stable with respect to $^{2}\Sigma$ NeH at the NeH⁺ geometry. However, the recent work of Gutowski and Simons³⁴ finds that this anion state is geometrically unstable with respect to Ne + H⁻. Thus it appears that both NeH and NeH⁻ are geometrically unstable as Rydberg or DR species.

E. CH,

Neither the Rydberg species CH₅ nor its DR CH₅-have been seen experimentally.¹⁰ Raynor and Herschbach² computed electric dipole transition moments

TABLE III. CAS MCSCF Geometries (Bond Length, au, and Bond Angle, deg) and Local Harmonic Frequencies (cm⁻¹) of H₂F⁺ and Two Lowest Geometrically Stable² Rydberg States of FH₂

| | cation | ² B ₂ neutral | ² B ₁ neutral | |
|--------------------|--------|-------------------------------------|-------------------------------------|--|
| r (F-H) | 1.827 | 2.316 | 1.818 | |
| angle | 112.7 | 97.0 | 112.5 | |
| A _t vib | 1482 | 1473 | 1496 | |
| $\mathbf{B_2}$ vib | 3563 | 4150 | 3633 | |
| A_1 vib | 3542 | 1025 | 3601 | |

^aThe ²A₁ ground state of the neutral is geometrically unstable.

among several Rydberg states at the geometry of the CH_5^+ cation, but they did not examine the geometrical stability of any of the CH_5 Rydberg states. Gutowski, Simons, Hernandez, and Taylor¹ and subsequently Gutowski and Simons³⁴ studied both CH_5 and CH_5^- and found several DR states that are candidates for Feshbach resonances. However, the latter workers find both the ground state of Rydberg CH_5 and the DR state of CH_5^- to be geometrically unstable with respect to fragmentation. Cremer and Kraka²9 studied CH_5^- , but did not examine its local geometrical stability or lack thereof; they did consider the overall thermodynamic stability of this species and predicted it to be unstable by 54.5 kcal/mol with respect to H⁻ + CH_4 .

F. H₂F

The only evidence for metastable states of D₂F comes from the Raksit, Jeon, and Porter neutralized ion beam experiments.46 Petsalakis, Theodorakopoulos, Wright, and Hamilton,⁴⁷ in 1988, and Gutowski and Simons,³⁴ in 1989, examined the ground and low-lying excited states of this species and found the ground state to be geometrically unstable, while some bound excited states were predicted to exist. Geometries and harmonic vibrational frequencies for H₂F⁺ and for the two lowest geometrically stable states of H₂F (²B₂(2b₂) and ²B₁-(2b₁)) are presented in Table III. The geometries of the ²B₂ state and the cation are very different, as are the vibrational frequencies. The reason is that the neutral's 2b2 orbital is dominated by an antibonding combination of hydrogens' s-type orbitals rather than by a nonbonding fluorine np_{ν} symmetry orbital. This antibonding interaction is responsible for a dramatic elongation of the FH bonds (by 0.5 au) and a reduction of the symmetric stretching frequency (by 2500 cm⁻¹). Therefore, we see that the lowest geometrically stable state of FH₂ is not a typical Rydberg state. However, the next excited state, the ²B₁(2b₁) state, is the first representative of the Rydberg family for FH2. It has a geometry and vibrational frequencies quite like those of its parent cation (see Table III). Electric dipole transition moments among certain states of H₂F were calculated by Raynor and Herschbach² and by Petsalakis et al.47

In 1986, Cremer and Kraka²⁹ looked at the H_2F^- DR species near the geometry of its parent cation. They found DR H_2F^- to be thermodynamically unstable with respect to $HF + H^-$ by 37.9 kcal/mol. Gutowski, Simons, Hernandez, and Taylor¹ studied the ground and excited states of DR H_2F^- and identified several excited states as candidates for Feshbach resonances. Subsequently, Gutowski and Simons³⁴ as well as Ortiz⁴8 found the ground state of H_2F^- to be geometrically unstable

in the vicinity of the parent cation equilibrium geometry.

G. Other DR Systems

The DR systems involving a third-row heavy atom were studied by Ortiz.⁴⁸ The $SH_3^-(C_{3v})$ and $ClH_2^-(C_{2v})$ structures were found to be geometrically unstable in their ground states. For PH_4^- a stable tetrahedral structure was found with a PH distance of 2.72 au and detachment energy of 0.38 eV. Another structure, with C_{2v} geometry and detachment energy of 0.95 eV was also found.⁴⁸ After including zero-point energy corrections, the C_{2v} structure was predicted to be 1.45 eV more stable than the DR isomer.

III. Autodetachment Lifetimes of Metastable DR States

In addition to these energetic and structural studies on NeH⁻, H_2F^- , H_3O^- , H_4N^- , and H_5C^- , the authors have undertaken an investigation⁴⁹ of the lifetimes with respect to electron detachment of various excited DR states of H_2F^- and are extending this study to the other DR anions covered in this review.

In using the stabilization method⁵⁰ to compute the energies and lifetimes of metastable Feshbach, shape, and core-excited shape (CES) resonances, one must find a large number of eigenvalues of the hamiltonian matrix H belonging to the DR anion's electronic configuration space. The lowest root of this H matrix corresponds to the electronically bound H_2F - state for the example at hand. Many of the next eigenvalues correspond to "scattering states" which describe a Rydberg neutral H_2F coupled to a continuum orbital containing an unbound electron. Among this multitude of such scattering states are the desired metastable states. The stabilization method provides a tool for finding the metastable states that are buried in the continuum.

To effect the stabilization technique, one finds all of the eigenvalues of H within some specified energy range of interest. This calculation is carried out over and over as the exponents (α_i) of all of the diffuse Rydberg-type basis functions used in the calculation are varied by a uniform "scale factor". This orbital exponent scaling corresponds to varying the radius of the orbitals and hence of the region of space within which the electrons are constrained. Constraining the electrons of a bound state should have no effect on such a state as long as the region to which they are constrained is large enough to contain the vast majority of their (square integrable) charge density.

In contrast, constraining a continuum state to any finite region of space amounts to placing it in a "box" and thus forcing its oscillatory function to match boundary conditions imposed by the box. This amounts to forming discrete states in place of the continuum. As the "box radius" is increased (i.e., as the orbital exponents are uniformly decreased), the energies of all such continuum states decrease.

As the orbital exponents of the diffuse basis functions are scaled, one finds a pattern in the eigenvalues of the H matrix such as shown in Figure 9. This data depict a situation in which the energy of an electronic configuration of symmetry ${}^{1}A_{1}(6a_{1}^{2})$ remains rather constant as the α_{i} are scaled until a continuum configura-

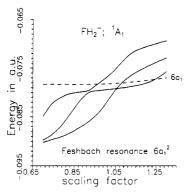


Figure 9. Stabilization plot for the longest-lived Feshbach ${}^{1}A_{1}(6a_{1}^{2})$ resonance. The energy of the nearby neutral state is depicted by dashed line.

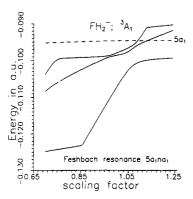


Figure 10. Stabilization graph for the two-open-channel Feshbach ${}^3A_1(5a_1na_1)$ resonance. The energy of the nearby neutral state is depicted by dashed line.

tion of the same symmetry approaches from "below" as the box size is made smaller (i.e., as the α_j are increased). As the two configurations approach, they are coupled via the electronic hamiltonian (i.e., they are both used in forming the H matrix) and they undergo an avoided crossing.

These avoided crossings characterize the nature of the metastable states; these states consist of a superposition of continuum and bound electronic configurations. The strength of the coupling between the configurations influences the lifetime of the metastable state. Building on Simons' original treatment⁵¹ of this problem, Frey and Simons demonstrated⁵² in 1986 how such lifetimes could be extracted from the "avoided crossings" that occur in stabilization plots.

The present authors used this technique to compute the lifetimes of several singlet and triplet Feshbach and core-excited shape resonances of the A_1 , B_1 , B_2 , and A_2 states of $H_2F^{-.49}$ Shape resonances that lie just above the (geometrically unstable) 2A_1 ground state of the neutral were not observed. Several of the pertinent stabilization graphs are shown in Figures 9–13 (where the energies relative to those of the parent cations are displayed in Hartree units (27.21 eV)), and the resulting state symmetries, energies, and lifetimes are given in Table IV.

The longest lived Feshbach resonance is of ${}^{1}A_{1}(6a_{1}{}^{2})$ symmetry (Figure 9) and its lifetime is 34×10^{-14} s. Among the five Feshbach resonances that we found, three have been classified as two-open-channel species, (see Figures 10 and 11 and Table IV). The ${}^{3}A_{1}(5a_{1}na_{1})$ resonance (Figure 10) can decay via ejection of an

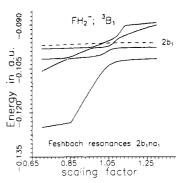


Figure 11. Stabilization graphs for two two-open-channel Feshbach ${}^3B_1(2b_1na_1)$ resonances. The energy of the nearby neutral state is depicted by dashed line.

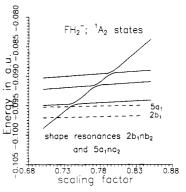


Figure 12. Three-term cluster of CES 1A_2 resonances. The two lower resonances are dominated by $2b_1nb_2$ electron configurations. The highest one has $5a_1na_2$ character. The middle one is the longest lived CES resonance. The energies of nearby neutral states $2b_1$ and $5a_1$ are depicted by dashed lines.

TABLE IV. Metastable State Symmetries, Types, Energies, and Lifetimes for Double Rydberg H₂F

| Energies, and Lifetimes for Double Kydberg H2r | | | | |
|--|-------------------|---|---------------------|-----------------------|
| symmetry | type ^a | configuration ^b | energy ^c | lifetime ^d |
| ¹ A ₁ | CES | $2b_2nb_2$ | -0.12369 | 3 |
| ¹ A, | CES | $2b_2nb_2$ | -0.11933 | 7 |
| $^{1}\mathbf{A}_{1}$ | F | $6a_1^2$ | -0.079 17 | 34 |
| ³ A₁ | CES | $2b_2nb_2$ | -0.12513 | 14 |
| ³ A ₁ | CES | $2b_2nb_2$ | -0.12326 | 32 |
| $^{3}A_{1}$ | F | 5a ₁ na ₁ | | |
| | | (4a ₁ ka ₁ channel) | -0.09886 | 1 |
| | | $(2b_2kb_2 channel)$ | -0.09881 | 5 |
| $^{1}A_{2}$ | CES | $2b_1nb_2$ | -0.09471 | 14 |
| ¹A, | CES | $2b_1nb_2$ | -0.091 57 | 80 |
| $^{1}A_{2}$ | CES | $5a_1na_2$ | -0.08946 | 26 |
| ³ A ₂ | CES | $2b_1nb_2$ | -0.094 26 | 18 |
| ${}^{3}\mathbf{A}_{2}$ | CES | $2b_1nb_2$ | -0.091 59 | 19 |
| 3A_2 | CES | 5a ₁ na ₂ | -0.089 59 | 24 |
| ¹ B ₁ | F | $2b_1na_1$ | -0.10069 | 4 |
| ${}^3\mathbf{B_1}$ | CES | $2b_2na_2$ | -0.12339 | 17 |
| ${}^{3}\mathbf{B}_{1}^{2}$ | F | $2b_1na_1$ | | |
| | | $(2b_2ka_2 channel)$ | -0.101 45 | 8 |
| | | (4a ₁ kb ₁ channel) | -0.10255 | 1 |
| 3B_1 | \mathbf{F} | $2b_1na_1$ | | |
| | | (2b ₂ ka ₂ channel) | -0.097 82 | 10 |
| | | (4a ₁ kb ₁ channel) | -0.09796 | 6 |
| ³ B₁ | CES | $2b_1na_1+5a_1nb_1$ | -0.090 25 | 17 |
| ${}^{3}\mathbf{B}_{2}$ | CES | $2b_2na_1$ | -0.12580 | 11 |
| ${}^{3}\mathbf{B}_{2}$ | CES | $2b_2na_1$ | -0.12297 | 2 |
| ${}^{3}\mathbf{B}_{2}^{2}$ | CES | $2b_1na_2+5a_1nb_2$ | -0.09241 | 14 |
| ${}^{3}\mathbf{B}_{2}$ | CES | $2b_1na_2+5a_1nb_2$ | -0.09092 | 46 |
| $^{3}B_{2}^{2}$ | CES | $2b_1na_2+5a_1nb_2$ | -0.089 10 | 7 |

^a Feshbach (F) and core-excited shape (CES). ^b The notation nλ ($\lambda = a_1$, a_2 , b_1 , or b_2) is used to indicate that one Rydberg-type electron is distributed among many λ -symmetry orbitals. ^c The energies are given relative to the parent cation species (in hartrees) in all cases. ^d The lifetimes are given in units of 10^{-14} s. A lifetime of 10^{-14} s corresponds to an energy width of 0.066 eV in the resonance.

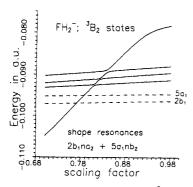


Figure 13. Three-term cluster of CES ³B₂ 2b₁na₂ + 5a₁nb₂ resonances. The energies of nearby neutral states 2b₁ and 5a₁ are depicted by dashed lines.

electron either to the ground ²A₁(4a₁) state of the neutral, or to the first excited ²B₂(2b₂) state. The former and the latter channels are reflected in Figure 10 in the steeply and less steeply rising branches of the stabilization graph, respectively. The slopes of these branches reflect the different kinetic energies of the ejected electron. In Figure 11, two other two-open-channel resonances of ³B₁(2b₁na₁) symmetry are displayed. For such two-open-channel cases, the total decay rate depends on the coupling of the resonant wavefunction with both open channels.

The CES resonances reported in Table IV frequently appear in clusters of two or three states, (see Figures 12 and 13). These clusters correspond to states of the same spatial and spin symmetry and are different solutions of the Schrödinger equation for the same neutral target states and with the same centrifugal barrier. The longest lived CES resonance is the ¹A₂(2b₁nb₂) state (Figure 12), with a lifetime of 80×10^{-14} s.

On the basis of the range of lifetimes found here, it is expected that electronically metastable states of FH₂⁻ can display vibrational and may even show some rotational structure. Since the ground states of the FH₂ anion and FH2 neutral are geometrically unstable near the cation equilibrium geometry, the observation of the CES and Feshbach resonances studied here could probably not be realized by using standard photoelectron or photodetachment techniques. However, experiments in which ground-state FH₂⁺ is used to produce, via double charge exchange, metastable states of FH₂ may be a fruitful avenue of approach. Alternatively, an approach using electron attachment to excited Rydberg states of neutral FH₂, which were predicted to be geometrically stable, may be successful.

As such, the experimental studies of DR states present significant challenges. The novelty of their electronic structures will hopefully provide sufficient incentive for experimentalists to examine the multitude of stable and metastable states that are predicted to occur.

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