Understanding Heterolytic Bond Cleavage

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Abstract: When considering the fragmentation of a single bond, the attractive singlet and repulsive triplet potential energy curves of the prototype $\text{H}_2 \rightarrow 2\text{H}$ dissociation often come to mind. For species in which homolytic bond cleavage is energetically favored, such comparisons are reasonable. For other species where heterolytic cleavage gives lower-energy products, the $\text{H}_2$ analogy is inappropriate. This paper offers a qualitative theoretical treatment of the singlet and triplet potential energy curves that arise when a single bond formed by an electron pair is cleaved either homolytically or heterolytically. This analysis is shown to provide insight into several problems involving transition metal systems: transition metal carbynyls, metal ion-ligand complexes, and transition metal dimers.

I. Introduction

As chemists, much of our intuition concerning chemical bonds is built on simple models introduced in undergraduate chemistry courses. The detailed examination of the $\text{H}_2$ molecule via the valence bond and molecular orbital approaches forms the basis of our thinking about bonding when confronted with new systems. Ordinarily, when we imagine bringing two radicals $\text{X}'$ and $\text{Y}'$ (each having a doublet spin state) together to form a single covalent bond, we anticipate that a bonding singlet state and a repulsive triplet state of the $\text{XY}$ molecule are formed, much as they are for $\text{H}_2$. However, we have recently encountered several systems in which this picture of the bonding is incomplete and for which this simple intuition has led to flawed analyses involving qualitatively incorrect potential energy surfaces.

These cases involve species that dissociate heterolytically; i.e., during cleavage of a covalent bond one of the fragments retains both bonding electrons and these fragments have energies below those where each fragment retains a single electron. Far from being unusual, a preference for heterolytic bond cleavage arises quite naturally in systems involving transition metals, where interactions between empty metal orbitals and two-electron donor ligands are ubiquitous. This situation is qualitatively different from the case of $\text{H}_2$, where the $\text{H}^+$ and $\text{H}^+$ asymptote lies at much higher energies than $\text{H}^+$ and $\text{H}^-$. The purpose of this paper is to outline how to correctly assess the qualitative characteristics of the potential energy surfaces involved in bonds that cleave heterolytically.

The theoretical methods and concepts included in this work are not new. Indeed, a series of articles by Pross and Shaik apply a valence-bond picture to explain the singlet-state potential energy surfaces that characterize a wide variety of prototypical organic reactions, including cation–anion recombination, donor–acceptor interactions, elimination reactions, and solution-phase $\text{S}_2$ reactions. This previous work demonstrates that the ideas discussed here have a very broad applicability. In the present paper, the roles of spin and permutational symmetry in determining which asymptotic states connect to which states of the $\text{XY}$ molecule are treated in more detail than in refs 1–5, and the results are directed at elucidating transition metal systems.

II. Summary of the State Correlations

To consider why the two-orbital, two-electron single bond formation case can be more complex than often thought, consider the $\text{H}_2$ system in detail. In the molecular orbital (MO) description of $\text{H}_2$, both bonding $\sigma_1$ and antibonding $\sigma^*$ MOs appear. There are two electrons that can both occupy the $\sigma_1$ MO to yield the $\Sigma_u^+(\sigma_1^2)$ ground electronic state; however, they can also occupy both MOs to yield $\Sigma_u^+(\sigma_1^2\sigma_1^2)$ and $\Sigma_u^-(\sigma_1^2\sigma_1^2)$, or both can occupy the $\sigma^*$ MO to give the $\Sigma_g^-(\sigma^*_1)$ state. As demonstrated explicitly in Appendix A, the former two states dissociate homolytically to $\text{X}^+ + \text{X}^- = \text{H}^+ + \text{H}^-$, and the latter two dissociate heterolytically to $\text{X} + \text{X}^* = \text{H}^+ + \text{H}^-$. (In all cases considered here, only two electrons play active roles in the bond formation. The symbols $\text{X}$, $\text{X}^*$, and $\text{X}^*$ are used to denote species in which neither one, or both bonding electrons, respectively, are attached to the $\text{X}$ fragment.) In the case of $\text{H}_2$ and for many other systems, the latter two states are sufficiently high in energy relative to the former two that they can be (and often are) ignored.

For several systems studied in our recent research, we have confronted situations where one of the heterolytic bond dissociation asymptotes ($\text{X}^+ + \text{Y}^*$ or $\text{X}^* + \text{Y}$) is lower in energy than the homolytic bond dissociation asymptote. In such cases, $\sigma$ bonding and $\sigma^*$ antibonding MOs are formed from the $\text{X}$ and $\text{Y}$ fragment.

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Supplementary Material Available: Branching-ratio plots for the reactions of $\text{H}_2\text{N}^+$, $\text{C}_2\text{H}_5^+$, $\text{PrNH}^+$, and $\text{CD}_2\text{O}^+$ with trimethyl phosphate, table of the results of acidity bracketing of (CH$_3$)$_2$PO$_2^-$, and table of heats of formation used in this work (9 pages). Ordering information is given on any current masthead page.


Figure 1. State correlation diagram for dissociation of a homonuclear species in which homolytic bond cleavage is energetically favored. Singlet surfaces are shown by solid lines and triplets by dashed lines.

Figure 2. State correlation diagram for dissociation of a homonuclear species in which heterolytic bond cleavage is energetically favored. Singlet surfaces are shown by solid lines and triplets by dashed lines.

Figure 3. State correlation diagram for dissociation of a heteronuclear species in which homolytic bond cleavage is energetically favored. Singlet surfaces are shown by solid lines and triplets by dashed lines.

Figure 4. State correlation diagram for dissociation of a heteronuclear species in which heterolytic bond cleavage to one product is energetically favored, but homolytic cleavage lies below the second heterolytic asymptote. Singlet surfaces are shown by solid lines and triplets by dashed lines.

orbits. As in the H2 case, occupying these two orbitals with two electrons gives rise to six electronic states: three singlets, 1Σg(σg2), 1Σg*(σg*2), and 1Σg**(σg**2), and a set of three degenerate triplets, 3Σu, 3Σu*, and 3Σu**.

When heterolytic bond cleavage is favored, the states that are analogues of the 1Σg+(σg+1) and 1Σg+(σu+1) states of H2 (the 1Σg and 1Σg** states) cannot be ignored in understanding the valence states of the XY molecules. The presence and character of these states are essential to a proper treatment of cases in which heterolytic bond cleavage is favored. Details necessary for understanding the relative energies of all six electronic states and to which separated asymptote they dissociate are outlined in Appendix A. For the homonuclear case, descriptions of the valence singlet and triplet Σ states are given in Figures 1 and 2 for situations in which covalent products lie below and above ionic products, respectively. The extensions of these state correlation diagrams to the heteronuclear situations are described in Figures 3 (when homolytic cleavage is favored), 4 (when X + Y is below X' + Y; which lies below X + Y'), and 5 (when X' + Y and X + Y; both lie below X' + Y'). A key feature in all five of these figures is that there is one and only one singlet surface that is an attractive (bonding) potential energy curve. The two other singlet surfaces are repulsive, as are the three triplet surfaces. The variations among the figures are due to mixing of the 1Σg, 1Σg*, and 1Σg** configurations (in the homonuclear cases, only the 1Σ and 1Σg** configurations mix since these have gerade symmetry while 1Σg* has ungerade symmetry), which varies with bond distance. As the energy ordering of the asymptotes varies from Figure 1 to 2 and from Figure 3 to 5, so do these correlations and so does the molecular state that connects to each asymptote. The characterization of repulsive surfaces in Figures 1–5 is based only on contributions to the interfragment interactions that arise from valence-orbital couplings. If one or both of the X and Y fragments possess a net charge, the qualitative potential surfaces described here are modified by any coulombic, charge-dipole, or charge-induced-dipole energies. Such additional factors can lead to attractive long-range interactions typical of ion–molecule complexes, and thereby modify the strictly repulsive character of the excited-state surfaces shown in Figures 1–5.

III. Application to Experimentally Studied Species

A. Photodissociation of Silicon–Silicon Bonds. As we were writing this paper, Michl published a short pedagogical paper based on ideas similar to those discussed here. His contribution focuses on why carbon–carbon bonds have a much larger singlet σ → σ* excitation energy than silicon–silicon bonds. In our terminology, such an excitation corresponds to a transition from the 1Σg+ surface to the 1Σg** surface of Figure 1; this is a case
in which the homolytic cleavage products lie lower in energy. The Michl article points out that this excitation energy is largely determined by the spacing between the homolytic and heterolytic dissociation asymptotes. Since the ionization energy of R₃Si is greater than that of R₃C, the gap between the homolytic and heterolytic dissociation products becomes lower for carbon-based species than for silicon–silicon bonded species.

**B. Transition Metal Carbonyls.** One class of intensely studied molecules where heterolytic bond cleavage is taken for granted is the transition metal carbonyls, M(CO)ₓ₊₁. Carbonyls are the quintessential two-electron donor ligands, and thus dissociation of a metal carbonyl complex along its ground electronic surface will involve heterolytic bond cleavage to form M(CO)ₓ₊₁ + CO = Y + X. This is shown in the qualitative schematic potential energy surface of Figure 6, taken from a recent study of manganese carbonyl cations by Dearden et al.⁷ Here, the M(CO)ₓ₊₁⁺ species (in either its ground or excited state) dissociates to form M(CO)ₓ⁺ + CO. Unfortunately, Figure 6 contains a fundamental mistake; namely, there can be no repulsive surface evolving from the dissociation asymptotes shown.

This can be seen by ascertaining the species involved in the other dissociation asymptotes. Homolytic cleavage of the Mn–CO bond corresponds to formation of Mn(CO)ₓ⁺ + CO⁺ and is much higher in energy than the Mn(CO)ₓ⁺ + CO asymptote since the ionization energy of the metal containing fragment is much lower than that of CO. The other heterolytic asymptote, Y⁺ + X, corresponds to generation of Mn(CO)ₓ⁺ + CO++, and is even higher in energy. Thus, Figure 4 shows the appropriate diagram for this system, as well as for all neutral, cationic and anionic metal carbonyls. (In neutral and anionic systems, homolytic cleavage corresponds to the high-energy products M(CO)ₓ⁺ + CO⁺ and M(CO)ₓ⁺ + CO++, respectively.)

The experimental work of Dearden et al. was designed to investigate how the spin state of the metal carbonyl might change with the number of ligands and how spin conservation might influence the bonding energetics and dissociation characteristics of these molecules. They considered that the repulsive curve shown in Figure 6 might be the result of a spin-forbidden dissociation process, and the crossing between the repulsive surface and the excited state attractive surface could therefore lead to a barrier to dissociation. The results of Figure 4 show that no repulsive surface can evolve from either Mn(CO)ₓ⁺ + CO asymptote, regardless of the spin of these species.

Experimentally, Dearden et al. found that there are no barriers for addition of CO to Mn(CO)ₓ⁺ (x = 1–5). This conclusion is, of course, not surprising given Figure 4, which provides a proper qualitative characterization of the potential energy curves. Our own discussion of dissociation in the Fe(CO)ₓ⁺ system.*

**C. Silver–Benzene Cation.** Another system where the analysis discussed above can be used to understand recent experimental data is the silver–benzene ion, (AgC₆H₆)⁺. Experiments by Willey et al.⁹ find that this complex photodissociates exclusively to Ag + C₆H₆ when irradiated with laser light over a photon range of 386–266 nm (3.21–4.66 eV). This observation is intriguing because the lower energy asymptote for dissociation is Ag⁺ + C₆H₆.

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neutral bond energy by noting that two Fe atoms in their $^3\text{D}(s^d^4)$ ground state cannot form a strong bond. Rather, ground-state Fe$_2$(s$^d^2$) correlates with association of two iron atoms in their $^2\text{F}(s^d^3)$ state, 0.86 eV higher in energy than the atomic ground state.\textsuperscript{17} (Note that heterolytic bond cleavage is unimportant here since this corresponds to Fe$^+ + \text{Fe}^+$, much higher in energy.)

In essence, formation of ground-state Fe$_2$ requires a promotion energy of 1.72 eV, such that the dissociation energy of the $\sigma^+_2$ bond is 2.87 eV relative to the 2 Fe($^2\text{F}$, s$^d^3$) asymptote.

In discussing the relatively higher bond energy for the Fe$^+$ dimer ion, Morse commented that the promotion energy for this charge state was only 0.86 eV since ground-state Fe$^+(d^6)$ already has a s$^d^4$ configuration.\textsuperscript{13} The implicit assumption here is that ground-state Fe$_2^+$(s$^d^2$) dissociates homolytically to Fe(s$^d^3$) + Fe(s$^d^3$), 0.86 eV above the Fe(s$^d^3$) + Fe(s$^d^3$) ground-state asymptote. As we have pointed out elsewhere,\textsuperscript{14} heterolytic cleavage of this ground-state dimer ion Fe(s$^d^3$) + Fe(s$^d^3$), lying only 0.23 eV above the ground-state asymptote. Relative to this asymptote, the dissociation energy of the $\sigma^+_2$ bond of Fe$^+$ is 2.95 eV, very similar to the value for the Fe$_2$ neutral. Thus, these promotion energy arguments quantitatively account for the large difference in the cationic and neutral dimer bond energies when the correct dissociation asymptotes are considered.

Complications. The details of the surfaces for Fe$_2^+$ and other transition metal dimers ions will, of course, be complicated by other considerations. When using the analysis much higher in energy (and treated in Appendix A) for homonuclear species that contain two electrons in two s-based orbitals and open d-shells, it is necessary to also consider the spin coupling and g and u symmetries of the states arising from the underlying d-based orbitals. As shown in Appendix B, for systems arising from atomic asymptotes of the form s$^d^2$ + s$^d^2$, s$^d^2$ + s$^d^3$ and s$^d^2$ + s$^d^3$ (note that the latter asymptote corresponds to M$^2+ + M^+$), it is possible to use our earlier analysis with the d$^*"$core electrons treated as X and the d$^*"$ core viewed as Y. As a result, the potential curves such as depicted in Figure 4 are expected when the s$^d^2$ + s$^d^3$ asymptote is the lowest. In addition, the d$^*"$ core species lies lowest. Likewise, Figure 1 applies when dealing with neutral homonuclear transition metal dimers where the homolytic asymptote of s$^d^2$ + s$^d^3$ configuration is lowest in energy.

Of course, this treatment assumes that the dominant part of the bonding and antibonding interactions arises from the s-based orbitals, and that the d$^*"$ core play no role except in determining the relative ordering of the s$^d^2$ + s$^d^3$, s$^d^2$ + s$^d^3$, and s$^d^2$ + s$^d^3$ asymptotes. This is most likely to be the case for late transition metal species for which the d orbitals are radially separated from the s orbitals. In reality, interactions between the open d shells on the atoms will give rise to potential surfaces that produce bands of states in place of the curves described here, although the qualitative behavior of these families of surfaces will be determined largely by the considerations outlined here.

Extension to Cases Involving One and Three $\sigma$ Electrons. For real transition metal dimers, surfaces involving two electrons in a $\sigma$ orbital will not fully represent the complexities since there will be additional surfaces corresponding to one or three $\sigma$ electrons. These will evolve from asymptotes corresponding to s$^d^2$ + s$^d^3$ and s$^d^2$ + s$^d^3$, respectively. In both cases and in the absence of d interactions, one attractive curve (corresponding to $\sigma^+_2$s$^d^2$(d$^*"$) and $\sigma^+_2$s$^d^2$(d$^*"$) $\sigma^+_2$s$^d^2$(d$^*"$) and $\sigma^+_2$s$^d^2$(d$^*"$) $\sigma^+_2$s$^d^2$(d$^*"$) $\sigma^+_2$s$^d^2$(d$^*"$) $\sigma^+_2$s$^d^2$(d$^*"$) $\sigma^+_2$s$^d^2$(d$^*"$) $\sigma^+_2$s$^d^2$(d$^*"$) $\sigma^+_2$s$^d^2$(d$^*"$) $\sigma^+_2$s$^d^2$(d$^*"$) $\sigma^+_2$s$^d^2$(d$^*"$) $\sigma^+_2$s$^d^2$(d$^*"$) $\sigma^+_2$s$^d^2$(d$^*"$) $\sigma^+_2$s$^d^2$(d$^*"$) $\sigma^+_2$s$^d^2$(d$^*"$) $\sigma^+_2$s$^d^2$(d$^*"$) $\sigma^+_2$s$^d^2(}$

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This simple picture is modified when the asymptotic \( s^2d\alpha^1 \) + \( s^2d\alpha^1 \) (or \( s^2d \) + \( s^2d \)) states are split into high- and low-spin coupled states, as they are for the \( Ni^+ \) case (\( ^2D \) versus \( ^2S \) states of \( Ni \)). Analogous considerations to those in the previous section can be used to analyze this situation. Here, the high-spin asymptotic states produce two sets of \( \sigma^1d\sigma^1 \alpha^1 \) (or \( \sigma^1d\alpha^1 \)) attractive curves and a set of \( \sigma^1d\sigma^1 \alpha^1 \) (or \( \sigma^1d^2 \)) repulsive curves. The higher energy low-spin asymptotic states produce another set of \( \sigma^1d\sigma^1 \alpha^1 \) (or \( \sigma^1d^2 \)) repulsive curves. Using the \( Ni + Ni^+ \) system as an example, the \( Ni(s^2d) + Ni(s^2d) \) asymptote produces a set of 100 bonding quartet \( \sigma^2d^2 \) states, a set of 100 antibonding quartet \( \sigma^2d^2 \) states, and a set of 100 bonding doublet \( \sigma^2d^2 \) states. The \( Ni(2D,s^2d) + Ni(2D,s^2d) \) asymptote produces a set of 100 antibonding doublet \( \sigma^2d^2 \) states and no bonding states. This pattern of potential energy curves is shown in Figure 8. A similar pattern would appear for the molecular states with three \( \sigma \) electrons, e.g., \( Ni \) \( (5F,s^2d) \) + \( Ni \) \( (5F,s^2d) \) versus \( Ni \) \( (5F,s^2d) \) + \( Ni \) \( (5F,s^2d) \) asymptotes in the \( Ni^+ \) case. This latter asymptote is not shown since it is higher in energy than those included in Figure 8.

Photodissociation of \( Ni^+ \). A case where this analysis allows the interpretation of recent experimental results is in the photodissociation of \( Ni_2Ar^+ \) as studied by Lessen and Brucat. 18 They found that this species dissociates primarily to \( Ni \) \( (3F,s^2d) \) at a photon energy of 2.98 eV, which is in agreement with recent ab initio calculations. 19 In contrast, homolytic cleavage leads to \( Co(s^2d) + Ni(s^2d) \), 0.45 eV above the ground-state asymptote, and \( Co(s^2d) + Ni(s^2d) \), 1.47 eV higher. 17 These asymptotes lead to both high- and low-spin repulsive surfaces. Overall, for a given \( d^2 \) core configuration, the surfaces will correspond to those shown in Figure 4.

Figure 8. Qualitative potential energy surfaces for \( Ni_2^+ \) including molecular states with one (dotted lines), two (solid lines), and three (dashed lines) \( \sigma \) electrons. Note that the surfaces for states with two \( \sigma \) electrons correspond to those shown in Figure 4.

Heteronuclear Transition Metal Dimer Ions. It should be noted that qualitative aspects of the above analysis for homonuclear transition metal dimer ions will persist for heteronuclear ions. For example, the ground-state dissociation asymptote for \( CoNi^+ \) is the heterolytic cleavage products \( Co(s^2d) + Ni(s^2d) \). The alternative heterolytic cleavage to form \( Co(s^2d) + Ni(s^2d) \) is 0.23 eV higher in energy. Both of the surfaces evolving from these asymptotes will be strongly attractive since they correspond to different \( d \) orbital configurations on the two different nuclei, \( e^2d^2 \) and \( e^2d^2 \), respectively. 20 In contrast, homolytic cleavage leads to \( Co(s^2d) + Ni(s^2d) \), 0.45 eV above the ground-state asymptote, and \( Co(s^2d) + Ni(s^2d) \), 1.47 eV higher. 17 These asymptotes lead to both high- and low-spin repulsive surfaces. Overall, for a given \( d^2 \) core configuration, the surfaces will correspond to those shown in Figure 4.

The extent of this behavior can be seen by considering the 36 heteronuclear diatomic ions that can be formed from the first-row transition elements Sc–Cu. As throughout this paper, considering only species involving a single two-electron bond, one finds that 22 of 36 heteronuclear diatomic ions cleave heterolytically and 14 cleave homolytically.

IV. Summary

When interpreting results of dynamic and spectroscopic experiments involving dissociative species, it is essential to know how dissociation should be strongly allowed and will lead to prompt dissociation to form \( Ni^+ \). Further, it seems likely that optical transitions at lower energies will not be strongly allowed since lower-lying molecular states correspond to \( s-d \) transitions, parity forbidden in the atom.

Therefore, we postulate that irradiation of \( Ni_2Ar^+ \) at 3.49 eV accesses this strong, dissociative transition. At a photon energy of 2.98 eV, no strongly repulsive states are easily formed and the \( Ni_2Ar^+ \) molecule dissociates primarily by \( Ar \) loss; the \( Ni^+ \) species thus formed does not couple strongly to predissociative states and thus has a long lifetime. Note that the 1.07-eV excitation energy to the homolytic dissociation asymptote is sufficient to quantitatively account for the difference between the bond energy of \( Ni^+ \) as measured by collision-induced dissociation versus that from the photodissociation study.

(21) Indeed, as pointed out to us by Professor M. D. Morse, states with different couplings of the \( d \) orbital configurations will also lead to families of attractive and repulsive curves. For example, \( Co \) in its \( 5F,5G,5D,5P \), or \( S \) states (all having an \( s^2d \) configuration) will interact with \( Ni(F,F,s^2d) \) along attractive potential curves. Repulsive curves will evolve from the corresponding \( Co(s^2d) + Ni(s^2d) \) and \( Co(s^2d) + Ni(s^2d) + Ni(s^2d) \) asymptotes. Similar considerations also hold for homonuclear transition metal systems.
the electronic states accessed in the experiment correlate to states of the fragment species. Since state-of-the-art quantum chemistry calculations cannot be performed routinely on all possible systems of interest, there is a need for qualitative means of describing the relevant low-energy potential energy surfaces. When dealing with homolytic bond rupture, this is often achieved by analogy with the potential curves of the H₂ molecule. Unfortunately, species containing transition metals often dissociate heterolytically, so the H₂ paradigm is inappropriate. We believe that the work described here provides a general framework for understanding many interesting bond-breaking problems, including those in which heterolytic bond rupture is favored. By applying our analysis to several systems of immediate experimental interest, and by pointing out qualitative errors in published potential energy surfaces, we attempt to illustrate the importance and utility of this framework.

Appendix A. Analysis of Two-Electron, Two-Orbital, Single-Bond Formation

A. Orbitals, Configurations, and States. The six electronic states involved in two-orbital, two-electron systems can be described in terms of the six configuration state functions (CSFs) that arise when one occupies the pair of bonding σ and antibonding σ* molecular orbitals with two electrons. The CSFs are combinations of Slater determinants formed to generate proper spin and spatial symmetry functions. The essential features of all Slater determinant wave functions are: (i) that they each involve a product of N spin orbitals and thus form an N-electron function, (ii) that the orbitals in the Slater determinant wave functions are: (i) that they each involve a product of N spin orbitals and thus form an N-electron function, (ii) that they embody permutational antisymmetry of the wave function, (iii) and that they are normalized functions of the coordinates of the N electrons.

To describe the singlet CSF corresponding to the closed-shell σ² orbital occupancy, a single Slater determinant

\[ 1\Sigma(0) = |\sigma\sigma\sigma\sigma\sigma\sigma\rangle = (2)^{-1/2}|\sigma(1)\sigma(2)\rangle - |\sigma(1)\sigma(2)\rangle \]

suffices. An analogous expression for the \( \sigma^2 \) CSF is given by

\[ 1\Sigma^*(0) = |\sigma\sigma\sigma^*\sigma^*\rangle = (2)^{-1/2}|\sigma(1)\sigma(2)\rangle - |\sigma(1)\sigma(2)\rangle \]

Also, the \( M_z = \pm 1 \) components of the triplet state having \( \sigma\sigma^* \) orbital occupancy can be written as single Slater determinants:

\[ 3\Sigma^*(1) = |\sigma\sigma\sigma^*\sigma^*\rangle = (2)^{-1/2}|\sigma(1)\sigma(2)\rangle - |\sigma(1)\sigma(2)\rangle \]
\[ 3\Sigma^*(2) = |\sigma\sigma\sigma^*\sigma^*\rangle = (2)^{-1/2}|\sigma(1)\sigma(2)\rangle - |\sigma(1)\sigma(2)\rangle \]

However, to describe the singlet CSF and \( M_z = 0 \) triplet CSF belonging to the \( \sigma\sigma^* \) occupancy, two Slater determinants are needed:

\[ 3\Sigma^*(0) = (2)^{-1/2}|\sigma(1)\sigma(2)\rangle - |\sigma(1)\sigma(2)\rangle \]

is the singlet CSF and

\[ 3\Sigma^*(0) = (2)^{-1/2}|\sigma(1)\sigma(2)\rangle + |\sigma(1)\sigma(2)\rangle \]

is the triplet CSF. In each case, the spin quantum number \( S_z \), its orbital angular momentum \( M_z \), and the Δ quantum number are given in the conventional \( \Delta \Lambda + 1 \) notation.

B. Orbital Correlations. The \( \sigma \) and \( \sigma^* \) molecular orbitals (MOs) are formed from orbitals of the constituent atoms or functional groups (denoted \( s_x \) and \( s_y \)). The energy variation in these orbital energies with \( X-Y \) separation gives rise to variations in the energies of the six electronic states that arise as combinations of the above CSFs. The homonuclear case, as \( R \) approaches \( \infty \), the energies of the \( \sigma \) and \( \sigma^* \) orbitals converge to the higher \( \sigma \) orbital energy. Unlike the homonuclear case, the \( \sigma \) and \( \sigma^* \) orbitals are not degenerate as \( R \to \infty \). The energy "gap" between the \( \sigma \) and \( \sigma^* \) orbitals at \( R = \infty \) depends on the electronegativity difference between the groups \( X \) and \( Y \). If this gap is small, it is expected that the behavior of this (slightly) heteronuclear system should approach that of the homonuclear \( X_2 \) and \( Y_2 \) systems.

C. State Correlation Diagrams. The three singlet, \( 1\Sigma(0) \), \( 1\Sigma^*(0) \), and \( 1\Sigma^*(0) \) \( \Sigma^* \) and \( 1\Sigma^* \) CSFs must be combined to form the three lowest energy valence electronic states of \( \Sigma \) symmetry. In the homonuclear case, all three single CSFs mix, while in the homonuclear case, the \( 1\Sigma^* \) CSF, with ungerade symmetry, does not couple with the \( 1\Sigma^* \) CSFs, which have gerade symmetry.

To understand the extent to which the \( \Sigma \) and \( 1\Sigma^* \) (and \( 1\Sigma^* \) for heteronuclear cases) CSFs couple, it is useful to examine the energies of these CSFs for the range of internuclear distances of interest \( R \), \( R < \infty \). Near \( R_n \), where the energy of the \( \sigma^* \) orbital is substantially below that of the \( \sigma^* \) orbital, the \( \sigma^* \) CSF lies significantly below the \( \sigma^* \) CSF which, in turn, lies below the \( \sigma^* \) CSF, the large energy splittings among these three CSFs simply reflecting the large gap between the \( \sigma \) and \( \sigma^* \) orbitals.

The \( 1\Sigma^* \) CSF generally lies below the corresponding \( 1\Sigma^* \) CSF by an amount related to the exchange energy between the \( \sigma \) and \( \sigma^* \) orbitals.

As \( R \to \infty \), the CSF energies are more difficult to "intuit" because the \( \sigma \) and \( \sigma^* \) orbitals become degenerate (in the homonuclear case) or nearly so (in the heteronuclear case). To pursue this point and arrive at an energy ordering for the CSFs appropriate to the \( R \to \infty \) region, it is useful to express each of the above CSFs in terms of the fragments' active orbitals \( s_x \) and \( s_y \) that comprise \( \sigma \) and \( \sigma^* \). To do so, the LCAO-MO expressions for \( \sigma \) and \( \sigma^* \):

\[ \sigma = C [s_x + s_y] \text{ and } \sigma^* = C^* [s_x - s_y] \]

are substituted into the Slater determinant definitions of the CSFs. Here \( C \) and \( C^* \) are normalization constants. The parameter \( \alpha \) is 1.0 in the homonuclear case and deviates from 1.0 in relation to the \( s_x \) and \( s_y \) orbital energy difference (if \( s_x \) lies below \( s_y \) then \( \alpha < 1.0 \); if \( s_x \) lies above \( s_y \), \( \alpha > 1.0 \)).

A decomposition of the six CSFs listed in section A, using the molecular orbitals introduced here yields:

\[ 1\Sigma(0) = C (s_x s_y s_x s_y) + z^2 (s_x s_y s_x s_y) + z^2 (s_x s_y s_x s_y) ] \]
\[ 1\Sigma^*(0) = C^* (z^2 s_x s_y s_x s_y) + z^2 (s_x s_y s_x s_y) + z^2 (s_x s_y s_x s_y) ] \]
\[ 1\Sigma^*(0) = CC^* (z^2) (s_x s_y s_x s_y) + z^2 (s_x s_y s_x s_y) + z^2 (s_x s_y s_x s_y) ] \]
\[ 3\Sigma^*(1) = CC^* (z^2) (s_x s_y s_x s_y) + z^2 (s_x s_y s_x s_y) ] \]
\[ 3\Sigma^*(1) = CC^* (z^2) (s_x s_y s_x s_y) + z^2 (s_x s_y s_x s_y) ] \]
\[ 3\Sigma^*(0) = CC^* (z^2) (s_x s_y s_x s_y) + z^2 (s_x s_y s_x s_y) ] \]

Clearly, the three \( 3\Sigma^* \) CSFs retain purely covalent character as \( R \to \infty \) because each determinant describes an \( X^+ Y^- \) electron distribution. In this large-R limit, \( 3\Sigma^* \) and \( 2\Sigma^* \) CSFs possess covalent, \( s_x s_y s_x s_y \), and \( s_x s_y s_x s_y \) components. (In the homonuclear limit, the \( 1\Sigma^* \) CSF is purely ionic.) These singlet CSFs combine to produce the three true singlet states \( \Psi \), one of which is a covalent function \( s_x s_y s_x s_y \), of \( X^+ Y^- \) character, and two ionic wave functions, \( s_x s_y s_x s_y \) and \( s_x s_y s_x s_y \), having \( X^+ Y^- \) and \( X^+ Y^- \) character, respectively. At other values of \( R \), these three CSFs will mix (in various amounts) to produce three energetically distinct singlet-state surfaces. Plots of these energies versus \( R \) are called state correlation diagrams, and are shown in Figure 3 for the case where

(22) Simons, J. Energetic Principles of Chemical Reactions; Jones and Bartlett: Boston, MA, 1983.
Appendix B. Symmetry Analysis for Homonuclear Species Containing d^4 d^{**} Cores and Two Electrons in s-Based Orbitals

The developments presented in Appendix A need to be extended somewhat to cover homonuclear cases in which open-shell d orbitals are also present. For homonuclear ionic (cation or anion) species, dissociation must lead to fragments that contain different numbers of electrons. Given two electrons in the s-based orbitals, one can have s^2d^n + s^2d^n, s^2d^n + s^2d^{**}, or s^2d^n + s^2d^{**} orbital occupancies on the fragments. For example, when Fe^+ dissociates, one can form the low-energy Fe(s^2d^6) + Fe^*(s^2d^7), the excited Fe^*(s^2d^6) + Fe(s^2d^5), or the very high-energy Fe^*(s^2d^6) + Fe(s^2d^4). Of course, other asymmetries such as the ground-state Fe(s^2d^6) + Fe^*(s^2d^5) occupy ancillary, and are of s^2d^n character. They are not included in the present analysis that focuses on states with two electrons in s-based orbitals.

To extend our earlier analysis to the cases discussed above, the following steps are followed:

1. The d^4 d^{**} d-orbital configurations are symmetry adapted to form g and u Slater determinant combinations:

\[ \psi_g = (2)^{-1/2}[s^2d^6 + d^{**}d^n] \]

\[ \psi_u = (2)^{-1/2}[s^2d^6 - d^{**}d^n] \]

where the notation d^4 d^{**}, for example, indicates that the atom on the left has a d configuration and the atom on the right has a d^{**} configuration.

2. The six configurations arising from s^2 s^2, s^2 s^1, and s^1 s^1 orbital occupancies (the former two being singlets and the latter producing three degenerate triplets and one singlet) are also combined into g and u Slater determinant symmetry functions:

\[ \psi_{s^2s^2}^{het} = (2)^{-1/2}[s^2s^2] \]

\[ \psi_{s^2s^1}^{het} = (2)^{-1/2}[s^2s^1] \]

\[ \psi_{s^2s^1}^{het} = (2)^{-1/2}[s^2s^1] \]

\[ \psi_{s^1s^1}^{homo} = (2)^{-1/2}[s^2s^2] \]

\[ \psi_{s^1s^1}^{homo} = (2)^{-1/2}[s^2s^1] \]

\[ \psi_{s^1s^1}^{homo} = (2)^{-1/2}[s^2s^1] \]

(N.B.: the two s orbitals refer to the orbitals on the left and right atoms) all of which are of g symmetry and contain heterolytic (het) and homolytic (homo) fragments, and

\[ \psi_{s^2s^2}^{homo} = [s^2s^2] \]

\[ \psi_{s^2s^1}^{homo} = [s^2s^1] \]

\[ \psi_{s^1s^1}^{homo} = [s^2s^2] \]

\[ \psi_{s^1s^1}^{homo} = [s^2s^1] \]

(3) the eight (one singlet g, three triplet g, one singlet u, and three triplet u) uu*2dnd^{**} antibonding molecular states; and

\[ \psi_{uu*2dnd^{**}}^{homo} = (2)^{-1/2}[s^2s^2] \]

\[ \psi_{uu*2dnd^{**}}^{homo} = (2)^{-1/2}[s^2s^1] \]

\[ \psi_{uu*2dnd^{**}}^{homo} = (2)^{-1/2}[s^2s^2] \]

all of which are of g symmetry; and

\[ \psi_{uu*2dnd^{**}}^{homo} = (2)^{-1/2}[s^2s^1] \]

\[ \psi_{uu*2dnd^{**}}^{homo} = (2)^{-1/2}[s^2s^1] \]

\[ \psi_{uu*2dnd^{**}}^{homo} = (2)^{-1/2}[s^2s^1] \]

all of which are of u symmetry. For the triplet states, one can form

\[ \Psi_{T,homo}^{u} = [s^2s^2][d^6d^{**} - d^6d^n] \]

and the corresponding \( M_s = -1 \) and 0 states which are of g symmetry, and

\[ \Psi_{T,homo}^{g} = [s^2s^2][d^6d^{**} + d^6d^n] \]

and the corresponding \( M_s = -1 \) and 0 states which are of u symmetry.

4. In principle, all of the above configurations of a given g, u, and of a given spin symmetry mix to produce the true electronic states of the corresponding symmetries. This mixing can, however, be anticipated by noting that there are two (one g and one u) singlet heterolytic states that contain only s^2d^n + s^2d^{**} configurations,

\[ (2)^{-1/2}[\psi_{het}^{g} + \psi_{het}^{u}] = (2)^{-1/2}[s^2d^n s^2d^{**} - s^2d^n s^2d^n] \]

\[ (2)^{-1/2}[\psi_{het}^{g} + \psi_{het}^{u}] = (2)^{-1/2}[s^2d^n s^2d^{**} - s^2d^n s^2d^n] \]

as well as two (one g and one u) singlet heterolytic states that contain only s^2d^n + s^2d^{**} configurations,

\[ (2)^{-1/2}[\psi_{het}^{g} - \psi_{het}^{u}] = (2)^{-1/2}[s^2d^n s^2d^{**} + s^2d^n s^2d^n] \]

\[ (2)^{-1/2}[\psi_{het}^{g} - \psi_{het}^{u}] = (2)^{-1/2}[s^2d^n s^2d^{**} + s^2d^n s^2d^n] \]

Configurations of the form s^2d^n + s^2d^{**} are represented by a total of eight homolytic states; two singlets

\[ \psi_{s^2s^2}^{homo} = (2)^{-1/2}[s^2s^2] \]

\[ \psi_{s^2s^1}^{homo} = (2)^{-1/2}[s^2s^1] \]

and two triplets (\( M_s = 1 \))

\[ \psi_{uu*2dnd^{**}}^{homo} = (2)^{-1/2}[s^2s^2] \]

\[ \psi_{uu*2dnd^{**}}^{homo} = (2)^{-1/2}[s^2s^1] \]

with their corresponding \( M_s = -1 \) and 0 functions.

Correlations for a species such as the Fe^+ ion discussed in the text, in which the s^2d^n + s^2d^{**} asymptote lies lowest, the s^2d^n + s^2d^{**} next, and s^2d^n + s^2d^{**} highest, are: (1) the two (one g and one u) s^2d^n + s^2d^{**} asymptotes correlate to the two (one g and one u) \( \sigma_{g,d^{**}} \) bonding molecular states; (2) the two (one g and one u) high-energy s^2d^n + s^2d^{**} asymptotes correlate to the two (one g and one u) \( \sigma_{u,d^{**}} \) antibonding molecular states; and (3) the eight (one singlet g, three triplet g, one singlet u, and three triplet u) s^2d^n + s^2d^{**} asymptotes correlate to the eight \( \sigma_{g,d^{**}} \) \( \sigma_{u,d^{**}} \) antibonding molecular states. Hence, one set (g and u) of attractive curves connecting to the low-energy heterolytic fragments, four sets (g and u) of repulsive curves connecting to the homolytic fragments, and one set (g and u) of repulsive curves connecting to the high-energy heterolytic fragments are expected in such cases. Such potential curves are illustrated in Figure 4.

In effect, if the d^4 core is viewed as X and the d^{**} core as Y, the results derived here are equivalent to those of Appendix A for heteronuclear systems, Figures 3–5.

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