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Unusual and Conventional Dative Bond Formation by s² Lone Pair Donation from Alkaline Earth Metal Atoms to BH₃, AlH₃, and GaH₃

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negatively charged H centers were suggested as a source of these unusual geometries. The other novel finding is that the electron affinities (EAs) of all six $M'-MH_3$ species lie in the 0.7–1.0 eV range, which is suggestive of ionic electronic structures for the neutrals even though the partial charges on the alkaline earth centers are as low as 0.3 atomic units. Partial positive charge on the alkaline earth atoms combined with substantial electron affinities of the BH₃, AlH₃, and GaH₃ groups, but only when distorted from planar geometries, were suggested to be the primary contributors to the large EAs.

I. INTRODUCTION

The elements of group 13 of the periodic table comprising boron, aluminum, gallium, indium, and thallium form many compounds with hydrogen. In particular, boron is capable of forming various hydrides such as trihydridoboron, BH₃, diborane $(B_2H_6)_{1}^{2}$ and decaborane $(B_{10}H_{14})^{1}$ in some of which bridging three-center bonds occur. Aluminum and gallium form fewer stable hydrides (alane (AlH₃) and polymeric $(AlH_3)_n$ derivatives; gallane (GaH_3) , digallane (Ga_2H_6) , and $(GaH_3)_n$ polymeric compounds^{1,3}) whereas the hydrides of indium and thallium are known mostly as fragments of complex compounds.^{1,2,4} Certain hydrides of boron, aluminum, and gallium have attracted attention primarily due to their usefulness in synthesis and materials chemistry. For example, borane (BH_3) is a reaction intermediate in the pyrolysis of diborane (leading to higher boranes¹), various boron hydrides are used as components in classical and secondary batteries and novel rechargeable storage systems⁵⁻¹¹ whereas alane (AlH₃) plays a reducing agent role in organic synthesis (as a selective reducer of many functional groups).¹² However, gallium hydrides are usually investigated in the context of properties exhibited by their adducts containing 4- or 5-coordinate gallium central atom(s)

and involving GaH_3 and monodentate or bidentate ligands.^{13,14} In addition, AlH_3 is a rocket fuel additive¹⁵ while various polymeric hydrides of boron, aluminum, and gallium remain active candidates for storing hydrogen.

Due to the fact that earlier literature reports describing the possibility of an excess electron binding by borane, alane, and gallane were contradictory (for BH₃),^{16–20} scarce and outdated (for AlH₃)^{21,22} or absent (for GaH₃), we recently investigated the issue of the stability of BH₃⁻, AlH₃⁻, and GaH₃⁻ anions.²³ In the course of our ab initio studies (based on a CCSD(T)/ aug-cc-pV5Z theoretical approach), we established the adiabatic electron affinity (EA) of BH₃ and the vertical electron detachment energy (VDE) of (BH₃)⁻ to be 0.02 and 0.04 eV, respectively, and confirmed the planar D_{3h} -symmetry structure of both neutral BH₃ and its daughter BH₃⁻ anion.

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Unlike BH₃⁻, AlH₃⁻ and GaH₃⁻ were found to adopt nonplanar geometries and to bind an excess electron more strongly (the EAs of AlH₃ and GaH₃ were calculated to be 0.31 and 0.26 eV, respectively, while the VDEs of AlH₃⁻ and GaH₃⁻ were evaluated to be 0.41 and 0.37 eV, respectively).²³

In our most recent paper,²⁴ we investigated compounds formed by an attachment of an alkaline earth metal atom (Be or Mg) to BH₃. We studied such a functionalization of the simplest borane mostly because we had become intrigued by the possibility of forming electronically stable anions by assembling two closed-shell species whose tendency to bind an excess negative charge is either zero (neither Be nor Mg forms a stable anion²⁵) or tiny (BH₃).²³ Our calculations revealed that the molecules assembled from these species are capable of forming electronically and thermodynamically stable BeBH₃⁻ and MgBH₃⁻ anions whose equilibrium structures are similar to those of their corresponding BeBH₃ and MgBH₃ neutral parents. Also, we found that the values of adiabatic electron affinity (1.11 eV) and vertical electron detachment energy (1.30 eV) predicted for BeBH3⁻ anion are significant and larger than those obtained for the MgBH₃⁻ anion (for which the EA of 0.68 eV and VDE of 0.74 eV were calculated). In addition, while investigating the structures of BeBH₃ and MgBH₃, we suggested that an alkaline earth metal atom forms a rather atypical bond with the boron atom. Namely, recalling that boron and its derivatives are well-known lone pair acceptors, we proposed to identify the Be-B and Mg-B bonds as dative bonds formed by the s² electron lone pair donation (coming from Be or Mg) to an empty 2p boron orbital of BH_3 . Due to the unusual nature of these bonds, we discussed them in terms of the NBO analysis (which led to the 0.8287(2s)Be + 0.5597(2p)B and 0.8693(3s)Mg + 0.4943(2p)B hybrid composition for the bonds in MgBH₃ and MgBH₃, respectively) and concluded that the bonding effects in BeBH₃ and MgBH₃ are primarily the result of the overlap of doubly occupied 2s Be orbital or 3s Mg orbital and an empty 2p B orbital.

With the intention of gaining a better insight into the bonding in the systems formed by assembling alkaline earth metal atom and the hydrides of 13 group elements as well as characterizing the structural changes accompanying the formation of these compounds, in this contribution we provide the results of detailed considerations regarding the electronic and thermodynamic stability of $M'BH_3$, $M'AlH_3$, and $M'GaH_3$ (M' = Mg, Ca) neutral molecules and their corresponding anions, established on the basis of correlated ab initio calculations using flexible atomic orbital basis sets.

II. METHODS

The equilibrium structures and corresponding harmonic vibrational frequencies of the closed-shell neutral MBH₃, MAlH₃, and MGaH₃ (M = Mg, Ca) molecules and their corresponding doublet anions were determined by applying the coupled-cluster method with single and double excitations $(CCSD)^{26-29}$ using the aug-cc-pVTZ basis set for Mg, B, Al, Ga, and H atoms³⁰ and the aug-cc-pVTZ-PP basis set for Ca.³¹ The electronic energies of the systems studied were then refined by employing the coupled-cluster method with the single, double, and noniterative triple excitations (CCSD(T)) method²⁶⁻²⁹ and the same basis sets. Both during the geometry optimizations followed by harmonic vibrational frequencies calculations with the CCSD method and while refining the electronic energies using the CCSD(T) method,

all orbitals in the core and valence shells have been correlated. For all of the structures considered here, all vibrational frequencies were real other than for the transition states we briefly mention where one frequency was imaginary.

The vertical electron detachment energies of the anions and the adiabatic electron affinities (not including zero-point vibrational corrections) of the neutral species were calculated by employing the supermolecular approach (i.e., by subtracting the energy of the anion from that of the neutral) involving the CCSD(T)/aug-cc-pVTZ/aug-cc-pVTZ-PP energies and by applying the outer valence Green function OVGF method (B approximation)³²⁻⁴⁰ together with the aug-cc-pVTZ and augcc-pVTZ-PP basis sets (again, all orbitals in the core and valence shells have been correlated during the OVGF calculations). Due to the fact that the OVGF approximation remains valid only for outer valence ionization for which the pole strengths (PS) are greater than 0.80-0.85,⁴¹ we verified that the PS values obtained were sufficiently large to justify the use of the OVGF method (the smallest PS for the states studied in this work was equal to 0.905).

The partial atomic charges were evaluated by the natural bond orbital (NBO) analysis scheme $^{42-46}$ using the CCSD electron densities, and all calculations were performed with the GAUSSIAN16 (Rev. C.01) package.⁴⁷

III. RESULTS

A. Geometries. When discussing the equilibrium structures of the neutral and anionic $M'-MH_3$ species (M' = Mg or Ca; M = B, Al, Ga), we refer to an angle θ (defined in Figure 1)



Figure 1. Definition of the θ angle that measures the distortion of the MH₃ unit's $C_{3\nu}$ -symmetry (pyramidal) structure away from planarity.

describing the deformation of the MX₃ fragment away from planarity. Positive values of θ are used to denote deformations in which the three M–H bonds are directed away from the alkaline earth atom and negative values of θ denote deformations in which the M–H bonds are directed toward the alkaline earth atom. It is the latter class of deformations that forms the unusual bonding paradigm referred to in our manuscript title; the former class constitutes the conventional paradigm.

A conventional dative bond involves donation of a lone electron pair from a Lewis base into an empty orbital of a Lewis acid as in, for example, H_3N-BH_3 . In such cases, the planar Lewis acid undergoes a change in valence orbital hybridization from sp² (with an empty p orbital) toward sp³, which thus gives rise to the distortion having positive θ . It is minimization of the electron repulsions between the donated partial electron pair and the M–H bonds' electrons that causes this change in hybridization. As we now demonstrate, there are additional electronic structure influences that come into play in some of the systems studied here that, for certain species, can produce forces that override these conventional hybridization factors and produce structures with negative θ values.







Figure 2. CCSD/aug-cc-pVTZ equilibrium structures (bond lengths in Å) of the neutral (left) and anionic (right) $MgMH_3$ (M = B, Al, Ga) systems.

In Figures 2 and 3 we show the global minimum-energy structures we identified for the six species formed by bonding either Mg or Ca to BH₃, AlH₃, or GaH₃ along with the structures of the anions formed by adding one electron. In searching for the lowest energy structures, we did consider geometries such as H-Mg-AlH₂ but in all cases such structures were found to be considerably higher in energy than those discussed here. In ref 23 we studied the BH₃, AlH₃, and GaH₃ fragments and their anions and in ref 24 we studied Be and Mg bonded to BH3 and the anions of these two complexes, and we will include some discussion of these species in the present work to offer comparisons. For some of the species, we also found higher energy local minima having θ values of opposite sign to those of our reported global minima. For example, for MgAlH₃ we found a negative θ local minimum 8 kcal/mol above our positive θ global minimum with a transition state 10 kcal/mol above the global minimum. For CaAlH₃ we found a positive θ local minimum 8 kcal/mol above our negative θ global minimum with a barrier 12 kcal/ mol above the global minimum. We did not explore these minima more because they lie above or very close to the energies of $M' + AlH_3$.

There are several features worth noting in these structures:

a. The most unusual feature occurs in CaAlH₃ and CaGaH₃ and in the CaBH₃⁻, CaAlH₃⁻, and CaGaH₃⁻ anions and presents as negative values for the distortion angle θ ; notice how the three B–H, Al–H, or Ga–H bonds bend toward rather than away from the Ca atom. The origin of this feature will be discussed in the next section.

Figure 3. CCSD/aug-cc-pVTZ-PP equilibrium structures (bond lengths in Å) of the neutral (left) and anionic (right) $CaMH_3$ (M = B, Al, Ga) systems.

- b. In all of the other neutral and anionic species, the distortion angle θ is positive as it is in conventional Lewis acid-base acceptor-donor pairs such as H₃B-NH₃.
- c. In all three of the Mg-containing species, the θ angle increases significantly in moving from the neutral to the anion.
- d. In the Ca-containing species involving Al and Ga, the θ angle becomes more negative in moving from the neutral to the anion and for CaBH₃ it moves from positive θ to negative θ in moving to the anion.
- e. For the neutral compounds containing B, the Mg–B or Ca–B bond lengths are very close to the sum of the B and Mg or Ca covalent radii⁴⁸ (0.84 Å for B, 1.41 Å for Mg and 1.76 Å for Ca). However, for the neutral compounds containing Mg and Al or Ga, the Mg to Al or Ga bond lengths are 0.3 Å or more longer than the sum of the covalent radii (1.21 Å for Al and 1.22 Å for Ga) while for the compounds containing Ca and Al or Ga, the Ca to Al or Ga bond lengths are at least 0.2 Å shorter than the sum of the covalent radii.

In the following sections, we will attempt to interpret these observations especially those involving the unusual bonding paradigm involving negative θ angles.

B. Probable Origin of Unusual Structures. To understand why CaAlH₃ and CaGaH₃ (and their anions as well as the CaBH₃⁻ anion) adopt the unusual geometries having negative θ values shown in Figures 2 and 3, let us examine the atomic partial charges extracted from our CCSD-level

calculations using the natural bond orbital method of Weinhold and co-workers.^{42–46} We will first focus on the six neutral molecules and then consider what happens when an extra electron is added. In Table 1 we show the atomic charges

Table 1. Partial Atomic Charges (in au) Calculated for BH₃, AlH₃, and GaH₃ by Employing the NBO Population Analysis Using CCSD Electron Densities

system	atom	atomic charges
BH ₃	В	0.354
	Н	-0.118
AlH ₃	Al	1.236
	Н	-0.412
GaH_3	Ga	0.984
	Н	-0.328

for the three electron acceptor MH_3 units in the absence of any alkaline earth atom and then we will compare these charge densities to those when the Mg or Ca atom is added.

Keeping in mind that H is slightly more electronegative than B, it is not surprising that the H atoms in BH_3 are slightly negatively charged. However, H is considerably more electronegative than Al or Ga as a result of which the H atoms in AlH₃ and GaH₃ are quite negatively charged. Also, keep in mind that BH_3 is a very poor electron acceptor (having an EA near zero) while AlH₃ and GaH₃ have modest EAs (near 0.3 eV).

Now, let us see what happens to the atomic charges on the MH_3 units' atoms when an Mg or Ca atom is attached. In Table 2 we show the partial atomic charges for the six M'-

Table 2. NBO Partial Atomic Charges (in au) Calculated Using CCSD Electron Densities for Mg–MH₃ and Ca–MH₃ and Changes in Charges (Δq) on MH₃ Atoms When Mg or Ca Is Added (for Neutral)

species	atom	atomic charges	Δq
MgBH ₃	Mg	0.503	
	В	-0.309	$\Delta q(B) = -0.66$
	Н	-0.065	$\Delta q(\mathrm{H}) = +0.05$
MgAlH ₃	Mg	0.300	
	Al	0.854	$\Delta q(\mathrm{Al}) = -0.38$
	Н	-0.385	$\Delta q(\mathrm{H}) = +0.03$
$MgGaH_3$	Mg	0.326	
	Ga	0.549	$\Delta q(\text{Ga}) = -0.44$
	Н	-0.292	$\Delta q(\mathrm{H}) = +0.04$
CaBH ₃	Ca	0.613	-
	В	-0.405	$\Delta q(B) = -0.76$
	Н	-0.069	$\Delta q(\mathrm{H}) = +0.05$
CaAlH ₃	Ca	0.975	
	Al	0.453	$\Delta q(\mathrm{Al}) = -0.78$
	Н	-0.476	$\Delta q(\mathrm{H}) = -0.06$
CaGaH ₃	Ca	0.996	-
	Ga	0.257	$\Delta q(\text{Ga}) = -0.73$
	Н	-0.418	$\Delta q(\mathrm{H}) = -0.09$

 MH_3 species (central column) as well as the differences (right column) between these atomic charges and those shown in Table 1 for the bare MH_3 units.

There are several features to note in these data:

a. There are only minor changes in the charges on the three H atoms when either an Mg or Ca atom is

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attached to BH₃, AlH₃, or GaH₃. As a result, the H atoms remain only weakly negatively charged in the BH₃-containing species but are still quite negatively charged in the AlH₃- and GaH₃-containing species.

- b. Most of the changes in atomic charges occur at the alkaline earth and B, Al, or Ga atoms and result from electron density flow from the ns^2 lone pair on the alkaline earth atom to the B, Al, or Ga atom. Of course, this is not surprising and the donor \rightarrow acceptor electron pair donation phenomenon is expected in such cases.
- c. The donor \rightarrow acceptor bond formation renders B negative in the first and fourth compounds but leaves Al or Ga positively charged in the other compounds.
- d. The magnitude of the electron density flow is considerably larger in the Ca-containing species than in the Mg-containing species especially when the MH_3 unit contains Al or Ga; this likely reflects the considerable difference in the two atoms' ionization potentials (7.6 eV for Mg and 6.1 eV for Ca).

On the basis of these atomic partial charges, we suggest the following reason behind the unusual (i.e., negative θ values) geometries found for neutral CaAlH₃ and CaGaH₃. In these two cases, there exist very strong Coulomb stabilization energies acting to attract the alkaline earth atom toward the

Table 3. Coulombic Interaction Energies Computed fromEq 1 Using the Atomic Partial Charges Given in Table 2

species	M′–H distance (Å)	Coulombic energy (eV)
MgBH ₃	2.737	-0.52
MgAlH ₃	3.488	-1.43
$MgGaH_3$	3.364	-1.22
CaBH ₃	2.955	-0.62
CaAlH ₃	2.238	-8.96
CaGaH ₃	2.255	-7.98

three equivalent H atoms. To illustrate this point in Table 3, we show the Coulombic energies computed as

$$C = \sum_{J=1}^{3} \frac{14.4q_{\rm H_{J}}q_{\rm M'}}{R_{\rm M'-H_{J}}} \, \rm eV$$
⁽¹⁾

where $R_{M'-H_j}$ is the distance in Å from the alkaline earth atom M' to the Jth H atom and $q_{M'}$ and q_{H_j} are the partial charges on these atoms, respectively.

Clearly, the cases of CaAlH₃ and CaGaH₃ are unique in the size of the Coulomb energies. We suggest it is these strong interatomic attractions that give rise to the unusual (negative θ) geometries observed in these two cases. For the other four species, there certainly are non-negligible Coulomb attractions between the alkaline earth atoms and the H atoms. However, it appears that these attractions are not strong enough to overcome the influence of the dative bond between the alkaline earth atom and the B, Al, or Ga atom. As explained earlier, this kind of conventional donor \rightarrow acceptor bonding acts to rehybridize the B, Al, or Ga atom away from sp² toward sp³ hybridization and thus to positive θ .

It might occur to the reader that some other influence is giving rise to the negative θ geometries and that the large partial charges then arise from that influence. However, we do not believe this is the case; we think it is the large partial

charges that cause the negative θ values, and we base this opinion on two observations:

- 1. From Table 1 we see that the partial charges on the H atoms of AlH₃ and GaH₃ are already (i.e., in their planar geometries with no Mg or Ca atom attached) quite substantial (-0.3 to -0.4), and we see from Table 2 that they increase in magnitude very little when a Mg or Ca atom is attached and the geometry evolves to negative θ . So, there is no evidence that the charges that we claim give rise to the large Coulomb attractions become large as θ evolves to negative values; they already were large and changed little as θ varied.
- 2. From Table 2 we also see that the partial charges on the Ca atoms in CaAlH₃ and CaGaH₃ are much higher than in the other species. It appears that a combination of the already-existing large negative charges on the H atoms of AlH₃ and GaH₃ and the large positive charges on the Ca atoms in CaAlH₃ and CaGaH₃ are what brings these two species into the realm of negative θ . Certainly, for the other four species, attractive Coulomb interactions between the Mg or Ca atom and the three H atoms in the MH₃ unit exist (see Table 3) but these interactions are not sufficient to overcome the tendency of Lewis acid-base pairs to adopt the positive θ geometries.

C. Stability with Respect to Fragmentation. We also examined how stable the six Lewis base-acid complexes are toward dissociation into various fragments. In Table 4, we present the results of such studies.

For all six molecules, breaking apart into $M' + MH_3$ is the least endergonic with ΔG^{298} values ranging from 2 to 13 kcal/ mol; so these species are not very strongly bound even though there exists strong intramolecular Coulomb stabilizations. However, all six molecules are substantially more stable with respect to dissociation into either $M'H_2 + MH$ or $M'MH + H_2$.

Table 4. Gibbs Free Energies (ΔG^{298} in kcal/mol) Predicted for the Fragmentation Processes of the Neutral Systems by Using the CCSD(T)/aug-cc-pVTZ/aug-cc-pVTZ-PP Electronic Energies Including Zero-Point Energy Corrections, Thermal Corrections, and Entropy Contributions (at T = 298.15 K) Calculated at the CCSD/ aug-cc-pVTZ/aug-cc-pVTZ-PP Level

fragmentation path	ΔG^{298}	
$MgBH_3 \rightarrow Mg + BH_3$	7.08	
$MgBH_3 \rightarrow MgBH + H_2$	112.09	
$MgBH_3 \rightarrow MgH_2 + BH$	85.67	
$MgAlH_3 \rightarrow Mg + AlH_3$	2.30	
$MgAlH_3 \rightarrow MgAlH + H_2$	21.67	
$MgAlH_3 \rightarrow MgH_2 + AlH$	77.04	
$MgGaH_3 \rightarrow Mg + GaH_3$	3.55	
$MgGaH_3 \rightarrow MgGaH + H_2$	23.54	
$MgAlH_3 \rightarrow MgH_2 + GaH$	160.84	
$CaBH_3 \rightarrow Ca + BH_3$	11.75	
$CaBH_3 \rightarrow CaBH + H_2$	71.75	
$CaBH_3 \rightarrow CaH_2 + BH$	154.25	
$CaAlH_3 \rightarrow Ca + AlH_3$	13.25	
$CaAlH_3 \rightarrow CaAlH + H_2$	27.37	
$CaAlH_3 \rightarrow CaH_2 + AlH$	151.90	
$CaGaH_3 \rightarrow Ca + GaH_3$	10.93	
$CaGaH_3 \rightarrow CaGaH + H_2$	25.69	
$CaGaH_3 \rightarrow CaH_2 + GaH$	232.12	

In our earlier work,²⁴ we found that BeBH₃ dissociating into Be + BH₃ had a ΔG^{298} of 10.68 kcal/mol.

D. Negative lons. We also examined what happens when an excess electron is added to these six species to form molecular anions. Recall that the Mg and Ca atoms have zero and very small (0.04 eV) EAs, respectively, and that the EAs of BH₃ (ca. 0 eV), AlH₃ (0.3 eV), and GaH₃ (0.3 eV) are also quite small. Nevertheless, the EAs and vertical electron detachment energies (VDEs) of the six molecules studied here turn out to be substantial, as shown in Table 5.

Table 5. Adiabatic Electron Affinities (EA in eV Not Including Zero-Point Energy Corrections) of the Neutral Systems and Vertical Electron Detachment Energies (VDE in eV) of Their Corresponding Anions Calculated at the CCSD(T)/aug-cc-pVTZ/aug-cc-pVTZ-PP Level (EA) and OVGF/aug-cc-pVTZ/aug-cc-pVTZ-PP Level (VDE) for the Equilibrium Structures Obtained by Employing the CCSD/ aug-cc-pVTZ/aug-cc-pVTZ-PP Theoretical Approach

	EA	VDE
$MgBH_3/(MgBH_3)^-$	0.675	0.914
$MgAlH_3/(MgAlH_3)^-$	0.930	1.206
MgGaH ₃ /(MgGaH ₃) ⁻	0.865	1.227
CaBH ₃ /(CaBH ₃) ⁻	0.811	1.001
$CaAlH_3/(CaAlH_3)^-$	0.989	1.295
$CaGaH_3/(CaGaH_3)^-$	0.991	1.332

The fact that the EAs of the AlH_{3} - and GaH_{3} -containing compounds have EAs and VDEs ca. 0.2–0.3 eV larger than the BH_{3} -containing compounds likely relates to the fact that AlH_{3} and GaH_{3} have EAs about this same amount larger than the EA of BH_{3} .

Having found such large EAs for all of these molecules, we wanted to understand the origin of this outcome. Earlier,⁴⁹ we had observed that EAs of donor \rightarrow acceptor complexes could be altered by varying the degree of electron density flow from the donor to the acceptor. In those cases, the electron binding occurred at the positive (donor) end of the complex and the magnitude of the resulting EA was small and characteristic of dipole binding. However, the data shown in Table 5 do not support a similar perspective in these cases since the EAs are larger than is typical for dipole binding (e.g., ca. 0.1 eV); in fact, they are more similar to the EAs found for ionic molecules such as NaCl whose EA⁵⁰ is 0.727 eV.

To further search for the origins of the large EAs, we evaluated the atomic charge densities for the six anions using the same approach as discussed earlier and compared these charges to those in the corresponding neutral species. The point of this comparison was to consider where the excess electron's density accumulated and to perhaps understand why. The results are shown in Table 6.

Keep in mind that the atomic charge differences reflected in comparing the third and fifth columns of Table 6 result from the charge density of the anion's SOMO as well as changes in the other occupied orbitals accompanying addition of the electron. There are several things worth noting in these data:

a. For the first four compounds, adding an electron renders the alkaline earth atom essentially neutral while for the last two species the Ca atom remains highly positively charged. Considering the substantial ionization potentials of Mg (7.6 eV) and Ca (6.1 eV), adding electron density to the partially positively charged Mg or Ca

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Table 6. NBO Partial Atomic Charges Calculated Using CCSD Electron Densities for Neutral and Anion Species as Well as the Changes in Charges in Moving from the Neutral to the Anion

system	atom	neutral charges	atom	anion charges	Δq
$MgBH_3$	Mg	+0.503	Mg	+0.072	-0.431
	В	-0.309	В	-0.820	-0.511
	Н	-0.065	Н	-0.084	-0.019
$MgAlH_3$	Mg	+0.300	Mg	+0.036	-0.264
	Al	+0.854	Al	+0.194	-0.660
	Н	-0.385	Н	-0.410	-0.025
$MgGaH_3$	Mg	+0.326	Mg	+0.085	-0.241
	Ga	+0.549	Ga	-0.140	-0.689
	Н	-0.292	Н	-0.315	-0.023
$CaBH_3$	Ca	+0.613	Ca	+0.058	-0.555
	В	-0.405	В	-0.680	-0.275
	Н	-0.069	Н	-0.126	-0.057
$CaAlH_3$	Ca	+0.975	Ca	+0.789	-0.186
	Al	+0.453	Al	-0.046	-0.499
	Н	-0.476	Н	-0.581	-0.115
$CaGaH_3$	Ca	+0.996	Ca	+0.766	-0.230
	Ga	+0.257	Ga	-0.166	-0.423
	Н	-0.418	Н	-0.534	-0.125

centers could be one contribution to the EAs of the M'-MH₃ compounds.

b. Both the alkaline earth atoms and the group 13 atoms undergo substantial charge reductions while each of the three H atoms increase little (<0.1) in negative charge, and the group 13 atom gains negative charge even when it was already negatively charged in the neutral molecule prior to addition of the excess electron (e.g., as in MgBH₃ and in CaBH₃).

The latter observation in particular tells us that it is not the electrostatic potential existing within the neutral species that determines where the excess electron's density will accumulate because the partially negatively charged B atom becomes more negatively charged when an electron is added. So, we decided to examine the spatial distribution of the anions' SOMOs realizing that these orbitals strongly effect where the excess electron's density accumulates. In so doing, it is important to keep in mind that each SOMO is constrained to be orthogonal to all of its anion's underlying molecular orbitals.

In Figures 4 and 5 we show the HOMOs of the six neutrals as well as the SOMOs of the corresponding anions.

Before discussing the SOMOs, it is useful to analyze the spatial distributions and nodal patterns of the six HOMOs to which the corresponding SOMOs must be orthogonal.

For the first four species:

- a. The NBO analyses reveal that these four HOMOs consist (almost entirely) of Mg–M or Ca–M (M = B, Al, Ga) bonding hybrids with orbital occupancies approaching 2 e, namely: $0.8980(3s)_{Mg} + 0.4399(2p)_{B}$ (for MgBH₃), $0.9369(3s)_{Mg} + 0.3497(3p)_{Al}$ (for MgAlH₃), $0.9302(3s)_{Mg} + 0.3670(4p)_{Ga}$ (for MgGaH₃), and $0.8891(4s)_{Ca} + 0.4577(2p)_{B}$ (for CaBH₃).
- b. In addition, these bonding hybrids have orbital amplitudes centered on the three H atoms having the opposite sign as the alkaline earth ns orbital (also reflecting amplitude from the lobe of the group 13 p orbital directed away from the alkaline earth atom).



Figure 4. HOMO (for the neutral, left) and SOMO (for the anion, right) orbitals of the MgMH₃ (M = B, Al, Ga) systems.



Figure 5. HOMO (for the neutral, left) and SOMO (for the anion, right) orbitals of the CaMH₃ (M = B, Al, Ga) systems.

For the two remaining species, we note that there are clear differences in comparison to the first four molecules:

- a. The HOMOs consist largely of Ca 4s orbitals combined in a bonding manner with orbitals on the three H atoms.
- b. Al or Ga orbital amplitude localized away from the Ca atom. Because of the negative θ values in these two species, this amplitude might be assigned to an sp³ type hybrid orbital on the group 13 atom that has its major lobe directed away from the Ca atom and has its minor lobe directed toward the Ca atom and with a sign

consistent with bonding between the minor lobe and the Ca atom.

c. The NBO analysis describes these HOMOs as follows: The HOMO for CaAlH₃ is $0.848(3p)_{Al}$ lone pair and $0.529(LV(s))_{Ca}$ lone vacant orbital; for CaGaH₃ the HOMO is $0.831(4p)_{Ga}$ lone pair and $0.556(LV(s))_{Ca}$ lone vacant orbital. So, in both cases, the HOMO appears to be more of a lone pair type orbital that has amplitudes on both the Ca and group 13 atoms.

The qualitative differences between the HOMOs of the first four and latter two species is also consistent with the differences in internal Coulomb interactions discussed earlier as suggested sources of the negative θ values present in the latter.

Turning now to the anions' SOMOs, we note the following:

- a. All six SOMOs have one more node along the $C_{3\nu}$ axis than do the corresponding HOMOs; this reflects the fact that the SOMOs are orthogonal to the HOMO.
- b. For the first four compounds, the SOMO has most of its amplitude on the side of the Mg or Ca atom directed away from the group 13 atom.
- c. The SOMO of $CaBH_3^-$ is more similar to the SOMOs of the Mg-containing species than it is to the SOMOs of $CaAlH_3^-$ and $CaGaH_3^-$. We had anticipated that the SOMO of $CaBH_3^-$ would help us understand why this anion displays a (small) negative θ value while all of the Mg-containing species and their anions have positive θ values, but this anticipation was negated. However, we will have more to say about this issue below.
- d. For the CaAlH₃⁻ and CaGaH₃⁻ SOMOs much of their amplitudes is localized outside the intermetal region to the left of the Ca atom and to the right of the Al or Ga atom.

Recall that the issues we are attempting to understand are why the M'MH₃ species have large EAs and what causes the $CaBH_3^-$ anion to have a negative θ value. Earlier, we pointed out that, for the first four species, the partially positively charged Mg or Ca atom is rendered essentially uncharged when the excess electron is added, and we suggested this was likely one contribution to the large EAs of these molecules. To uncover an additional likely contribution, we re-examined BH₃, AlH₃, and GaH₃. As noted earlier, these molecules have EAs in the 0.0-0.3 eV range and their anions have VDEs²³ between 0.02 and 0.4 eV, all of which are quite small. However, if the geometries of these species are distorted to assume nonzero θ values, the VDEs increase drastically, as shown in ref 23. To illustrate, we calculated the VDE of BH_3^- at $\theta = -14^\circ$ (and using bonds lengths as in CaBH₃⁻) and obtained 0.28 eV. Doing likewise for AlH₃⁻ and GaH₃⁻ at $\theta = -40^{\circ}$ we obtained VDEs of 2.4 and 2.9 eV, respectively. Therefore, we suggest that a second contribution to the large EAs observed for all six compounds is likely the large VDEs of the highly distorted (i.e., having large negative θ values) AlH₃⁻ and GaH₃⁻ units occurring in CaAlH₃⁻ and CaGaH₃⁻.

In summary, for all six compounds there are two sites that offer strong electron attraction potential: the partially positively charged Mg^{q+} or Ca^{q+} site and the distorted BH_3 , AlH₃, or GaH₃ site. For all species but CaBH₃, more of the added electron's density ends up on the group 13 atom even when the alkaline earth site is quite positively charged as it is in CaAlH₃ and CaGaH₃ (where the Ca charge is ca. 1.0) and even when the group 13 atom is already negatively charged as in MgBH₃ and CaBH₃. It is the spatial distribution of the anions' SOMOs and the fact that the SOMOs have to be orthogonal to the other orbitals that reflect where the extra electron's density ends up. Any electron density added to the MH₃ site's M atom tends to increase the magnitude of that site's θ value because the MH₃⁻ anions' VDEs increase with increasing $|\theta|$ which is why CaAlH₃⁻ and CaGaH₃⁻ have larger negative θ values than do their respective neutrals. The one character for which we do not yet have a reasonable explanation is why CaBH₃⁻ has a negative θ value while its neutral has a positive θ .

In addition to finding that the anions studied here have large VDEs, it is also interesting to point out the substantial differences in the stabilities of the anions with respect to dissociation when compared to the neutrals, as shown in Table 7.

Table 7. Gibbs Free Energies (ΔG^{298} in kcal/mol) for Neutral and Anionic Systems Evaluated As Detailed in Table 4

	ΔG^{298}
$MgBH_3 \rightarrow Mg + BH_3$	7.08
$MgAlH_3 \rightarrow Mg + AlH_3$	2.30
$MgGaH_3 \rightarrow Mg + GaH_3$	3.55
$CaBH_3 \rightarrow Ca + BH_3$	11.75
$CaAlH_3 \rightarrow Ca + AlH_3$	13.25
CaGaH ₃ → Ca + GaH ₃	10.93
$MgBH_3^- \rightarrow Mg + BH_3^-$	24.26
$MgAlH_3^- \rightarrow Mg + AlH_3^-$	15.60
$MgGaH_3^- \rightarrow Mg + GaH_3^-$	17.41
$CaBH_3^- \rightarrow Ca + BH_3^-$	29.42
$CaAlH_3^- \rightarrow Ca + AlH_3^-$	28.10
$CaGaH_3^- \rightarrow Ca + GaH_3^-$	27.61

Notice that all of the anions are much more stable with respect to dissociation into the donor/acceptor pairs than are the neutrals. This is a result of the quite large EAs of the neutral donor \rightarrow acceptor molecules compared to the EAs of their corresponding donor and acceptor fragments.

IV. CONCLUSIONS

On the basis of the CCSD(T)/aug-cc-pVTZ/aug-cc-pVTZ-PP and OVGF/aug-cc-pVTZ/aug-cc-pVTZ-PP calculations performed for the M'BH₃, M'AlH₃, and M'GaH₃ neutral molecules and their corresponding anions (whose equilibrium structures were obtained at the CCSD/aug-cc-pVTZ/aug-cc-pVTZ-PP level of theory), we arrive at the following conclusions:

- 1. M'-MH₃ (M' = Mg or Ca; M = B, Al, or Ga) forms rather weak dative bonds connecting the alkaline earth and group 13 atoms (ΔG^{298} for dissociation ranges from 2.3 to 13.25 kcal/mol). The ΔG^{298} values for dissociation of the corresponding anions are considerably larger.
- 2. The bonds are stronger for Ca-containing compounds than for Mg-containing compounds, probably because Ca is a better electron pair donor than Mg (i.e., Ca has a lower ionization potential than Mg).
- 3. The bonds involve donation of an ns² electron pair on the alkaline earth atom into an empty n'p orbital on the group 13 atom for MgBH₃, MgAlH₃, MgGaH₃, and

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CaBH₃ and generate geometries with positive θ values (meaning the M–H bonds pucker away from the alkaline earth atom as expected).

- 4. For CaAlH₃ and CaGaH₃ the bonds seem to also involve considerable ionic character, which produces geometries with negative θ values (with the M–H bonds directed toward the alkaline earth atom) because the partially negatively charged H atoms are attracted to the partially positively charged Ca atom.
- 5. The distances between the alkaline earth and group 13 atoms are close to the sums of the covalent radii of the two atoms.
- 6. All six of the neutral species have large electron affinities (0.7-1.0 eV) and their anions have large vertical electron detachment energies (0.9-1.3 eV). As a result, and because the M' and MH₃ fragments have very small EAs, the corresponding M'-MH₃⁻ anions have much larger (positive) ΔG^{298} values for dissociation than do the M'-MH₃ neutrals.
- 7. Upon electron attachment to form the negative ions, small geometry changes take place except that the θ values become more negative for CaAlH₃⁻ and CaGaH₃⁻ and more positive for all the Mg-containing species and they evolve from slightly positive for neutral CaBH₃ to slightly negative for CaBH₃⁻.
- 8. We suggest that it is a combination of the substantial partial positive charges on the alkaline earth atoms and the strong VDEs of the distorted (having nonzero θ values) BH₃⁻, AlH₃⁻, and GaH₃⁻ anions that give rise to the large EAs and VDEs observed for all six compounds.

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Notes

The authors declare no competing financial interest.

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