

# Ab initio study of geometrically metastable multiprotonated species: $MH_n^{k+}$

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The geometries and stabilities relative to fragmentation of  $H_4O^{2+}$ ,  $H_4S^{2+}$ ,  $H_3F^{2+}$ ,  $H_3Cl^{2+}$ ,  $H_2Ne^{2+}$ ,  $H_2Ar^{2+}$ ;  $H_4F^{3+}$ ,  $H_4Cl^{3+}$ ,  $H_3Ne^{3+}$ ,  $H_3Ar^{3+}$ ;  $H_4Ne^{4+}$ , and  $H_4Ar^{4+}$  have been studied using the quadratic configuration interaction (with single and double excitations plus approximate triple excitations included) QCISD(T)/6-311G(2df,2p) method at second-order Møller-Plesset optimized geometries MP2(full)/TZP+ZPE/6-31G\*\*. All of the triply charged  $H_4F^{3+}$ ,  $H_4Cl^{3+}$ ,  $H_3Ne^{3+}$ , and  $H_3Ar^{3+}$  and more highly charged  $H_4Ne^{4+}$  and  $H_4Ar^{4+}$  ions, as well as doubly charged  $H_2Ne^{2+}$  were not found to possess local minima on their zero-point corrected ground state surfaces, although  $H_4Cl^{3+}$  is only slightly unstable. Tetrahedral ( $T_d$ ) structures for  $H_4O^{2+}$  and  $H_4S^{2+}$ , planar triangular ( $D_{3h}$ )  $H_3F^{2+}$ , triangular pyramidal ( $C_{3v}$ )  $H_3Cl^{2+}$  and bent ( $C_{2v}$ )  $H_2Ar^{2+}$  were found to be local minima on the respective ground state surfaces. The latter five species lie above their respective ion-plus-ion dissociation products by 61, 91, 111, 67, and 116 kcal/mol, and have barriers to dissociation of 38, 20, 12, 34, and 5 kcal/mol (all energies being zero-point corrected). Such multiply charged cations store a great deal of energy, which may be released by the addition of a single *extra* electron to form the corresponding cation of one less charge.

## I. INTRODUCTION

### A. Background

It is well known in chemistry that protons can exothermically attach to molecules and even to rare gas atoms (see Ref. 1, and references therein). Olah and others<sup>2,3</sup> have implicated the  $H_4O^{2+}$  and  $H_4S^{2+}$  dications as intermediates in proton-deuterium exchange reactions of isotopomeric hydronium and hydrosulfonium ions in so-called "magic acid"  $FSO_3D \cdot SbF_5$  and  $FSO_3H \cdot SbF_5 \cdot SO_2$ . Although small multiply charged ions are ubiquitous in aqueous solution, they are rarely observed to be stable in the gas phase where solvation energies are absent and where they are believed to undergo destruction by Coulomb explosion.

Large multiprotonated molecules may be thermodynamically stable even in the gas phase *if* their internal Coulomb repulsion energy can be made small (e.g., when the protons are attached to parts of the molecule that are distant from one another). In small gas-phase multiprotonated molecules  $MH_n^{k+}$  with a single "central" nonhydrogen atom, the Coulomb repulsion is expected to be very large, as a result of which such species might not be expected to be thermodynamically stable. However, when a cation of charge  $k$  is formed in which there are  $n$  ( $> k$ ) symmetry-equivalent bonds to the central atom, the  $k$  charges can be distributed over  $n$  atoms. The resultant internal Coulombic repulsion among *fractional* charges of magnitude  $\sim k/n$  may thus be low enough to render such species metastable. In such a case, a local minimum on the potential energy surface will occur as will a barrier to dissociation. In this article, we present results of our *ab initio* study of such multiply protonated small molecules.

### B. Earlier work on multiply protonated systems

The thermodynamic stabilities of  $H_2Ne^{2+}$ ,  $H_3F^{2+}$ ,  $H_4O^{2+}$ ,  $H_3Ne^{3+}$ ,  $H_4F^{3+}$ , and  $H_4Ne^{4+}$  to loss of one pro-

ton have been studied at the self-consistent field (SCF) level with double-zeta basis sets (SCF/DZ) by Kozmuta *et al.*,<sup>4</sup> who found all of these multiprotonated species to be thermodynamically unstable to loss of a proton. Tetrahedral  $H_4O^{2+}$ ,  $H_4F^{3+}$ ,  $H_4S^{2+}$ , and  $H_4Cl^{3+}$  were optimized at the SCF level using a 6-31\* basis set by Choi *et al.*<sup>5</sup> For  $H_4O^{2+}$  and  $H_4S^{2+}$ , *ab initio* calculations of the vibrational frequencies and of the energy barriers to dissociation were carried out at the SCF/6-31G\* level in Refs. 2 and 3. The  $H_4O^{2+}$  dication was found to be thermodynamically unstable by 59.2 kcal/mol, but its tetrahedral structure was identified<sup>2</sup> as a local minimum with a dissociation barrier of 39.4 kcal/mol. The  $H_4S^{2+}$  dication was also found<sup>3</sup> to be thermodynamically unstable (by 27.2 kcal/mol), with the tetrahedral structure being a local minimum with a dissociation barrier of 57.3 kcal/mol. These thermodynamic energies and barriers were found to not change significantly when electron correlation corrections were included. Specifically, at the SCF/6-31G\*-optimized geometries using fourth-order Møller-Plesset perturbation theory (MP4SDTQ/6-31G\*\*) the exothermicities and barriers were 43.9 and 52.9 kcal/mol for  $H_4O^{2+}$  and 25.2 and 59.2 kcal/mol for  $H_4S^{2+}$ .

### C. This work

In this study, we reexamined these species using more flexible basis sets and more systematic treatments of electron correlation. As a result of this study, we predict that several of these dications are metastable species which have reasonably high barriers to dissociation. These properties of the corresponding potential energy surfaces may make materials containing these cations interesting candidates for use in energy storage. As illustrated in Sec. III, the pent up energy of these species may be released by adding an extra electron (e.g., electrochemically or via photoinduced

charge transfer from a neighboring counter ion) to form the species with one lower positive charge.

## II. COMPUTATIONAL DETAILS

The geometries of  $\text{HNe}^+$ ,  $\text{H}_2\text{Ne}^{2+}$ ,  $\text{H}_3\text{Ne}^{3+}$ ,  $\text{H}_4\text{Ne}^{4+}$ ,  $\text{HF}$ ,  $\text{H}_2\text{F}^+$ ,  $\text{H}_3\text{F}^{2+}$ ,  $\text{H}_4\text{F}^{3+}$ ,  $\text{H}_2\text{O}$ ,  $\text{H}_3\text{O}^+$ ,  $\text{H}_4\text{O}^{2+}$ ,  $\text{HAr}^+$ ,  $\text{H}_2\text{Ar}^{2+}$ ,  $\text{H}_3\text{Ar}^{3+}$ ,  $\text{H}_4\text{Ar}^{4+}$ ,  $\text{HCl}$ ,  $\text{H}_2\text{Cl}^+$ ,  $\text{H}_3\text{Cl}^{2+}$ ,  $\text{H}_4\text{Cl}^{3+}$ ,  $\text{H}_2\text{S}$ ,  $\text{H}_3\text{S}^+$ , and  $\text{H}_4\text{S}^{2+}$  were first optimized employing analytical SCF gradients<sup>6</sup> with a polarized split-valence basis set [results at this level are denoted SCF/6-31G\*\* (Refs. 7-9)] and at the correlated MP2(full) level. The final optimized geometries were obtained using MP2(full) calculations with the triple-zeta plus polarization basis (TZP) of Huzinaga and Dunning (10s6p/5s3p) + 3d functions ( $\alpha_d = 0.88$  for O and 0.95 for F) for O and F (Ref. 9) and the McLean-Chandler (12s9p/6s5p) + 3d functions [ $\alpha_d = 0.65$  for S, 0.75 for Cl, and 0.85 for Ar (Ref. 10)]. The fundamental vibrational

frequencies, normal coordinates, and zero-point energies (ZPE) were calculated by standard FG matrix methods. Finally, correlated total energies were evaluated in the full fourth-order frozen-core approximation both by Møller-Plesset perturbation theory<sup>11</sup> (MP4) and by the quadratic configuration interaction including singles and doubles with approximate triples QCISD(T)<sup>12</sup> method using the 6-311G(2df,2p) standard basis sets. The GAUSSIAN 90 program suite<sup>13</sup> was used to perform all of the calculations whose results are discussed here.

## III. RESULTS AND DISCUSSION

Our calculated geometries (Table I), total energies at various levels of theory (Tables II and III), dissociation energies and barriers (Table IV), harmonic vibrational frequencies as well as infrared (ir) and Raman intensities and zero-point energies (ZPE) (Tables V) are given in Tables I-V. The calculated geometries of  $\text{H}_2\text{O}$ ,  $\text{H}_3\text{O}^+$ ,  $\text{H}_2\text{S}$ ,

TABLE I. Calculated and experimental geometries (Å and degrees).

Species	Symmetry	Method	$R(\text{M-H})$	HMH, angle
$\text{H}_2\text{O}, ^1A_1$	$C_{2v}$	SCF/6-31G**	0.943	106.0
		MP2(full)/6-31G**	0.961	103.9
		MP2(full)/TZP	0.962	105.1
		EXPT <sup>c</sup>	0.957	104.5
$\text{H}_3\text{O}^+, ^1A_1$	$C_{3v}$	SCF/6-31G**	0.961	114.7
		MP2(full)/6-31G**	0.979	112.6
		MP2(full)/TZP	0.980	112.6
$\text{H}_4\text{O}^{2+}, ^1A_1$	$T_d$	SCF/6-31G**	1.023	109.47
		MP2(full)/6-31G**	1.043	109.47
		MP2(full)/TZP	1.044	109.47
$\text{H}_4\text{O}^{2+}(\text{ts}), ^1A_1$	$C_{3v}$	SCF/6-31G**	2.064 <sup>a</sup>	
			0.985 <sup>b</sup>	110.9 <sup>c</sup>
		MP2(full)/6-31G**	2.158 <sup>a</sup>	
			1.004 <sup>b</sup>	111.5 <sup>c</sup>
		MP2(full)/TZP	2.144 <sup>a</sup>	
$\text{H}_2\text{S}, ^1A_1$	$C_{2v}$	SCF/6-31G**	1.327	94.4
		MP2(full)/6-31G**	1.329	92.8
		MP2(full)/TZP	1.333	92.1
		EXPT	1.336	92.06
$\text{H}_3\text{S}^+, ^1A_1$	$C_{3v}$	SCF/6-31G**	1.335	97.1
		MP2(full)/6-31G**	1.339	95.8
		MP2(full)/TZP	1.346	94.9
$\text{H}_3\text{S}^+, ^1A_1'$	$D_{3h}$	SCF/6-31G**	1.322	120.
		MP2(full)/6-31G**	1.324	120.
		MP2(full)/TZP	1.330	120.
$\text{H}_4\text{S}^{2+}, ^1A_1$	$T_d$	SCF/6-31G**	1.360	109.47
		MP2(full)/6-31G**	1.366	109.47
		MP2(full)/TZP	1.378	109.47
$\text{H}_4\text{S}^{2+}(\text{ts}), ^1A_1$	$C_{3v}$	SCF/6-31G**	2.772 <sup>a</sup>	
			1.344 <sup>b</sup>	117.1 <sup>c</sup>
		MP2(full)/6-31G**	2.822 <sup>a</sup>	
			1.349 <sup>b</sup>	117.8 <sup>c</sup>
		MP2(full)/TZP	2.830 <sup>a</sup>	
$\text{HF}, ^1\Sigma^+$	$C_{\infty v}$	SCF/6-31G**	0.901	
		MP2(full)/6-31G**	0.921	
		MP2(full)/TZP	0.925	
		EXPT	0.917	118.2 <sup>c</sup>
$\text{H}_2\text{F}^+, ^1A_1$	$C_{2v}$	SCF/6-31G**	0.944	115.9
		MP2(full)/6-31G**	0.966	112.7

TABLE I. (Continued.)

Species	Symmetry	Method	$R(M-H)$	HMH, angle
$H_3F^{2+}, ^1A_1$	$D_{3h}$	MP2(full)/TZP	0.968	113.0
		SCF/6-31G**	1.047	120.
		MP2(full)/6-31G**	1.073	120.
$H_3F^{2+}(ts), ^1A_1$	$C_{2v}$	MP2(full)/TZP	1.071	120.
		SCF/6-31G**	1.581 <sup>a</sup>	
			0.995 <sup>b</sup>	113.7 <sup>c</sup>
		MP2(full)/6-31G**	1.639 <sup>a</sup>	
$HCl, ^1\Sigma^+$	$C_{\infty v}$		1.018 <sup>b</sup>	112.5 <sup>c</sup>
		MP2(full)/TZP	1.648 <sup>a</sup>	
			1.021 <sup>b</sup>	115.5 <sup>c</sup>
		SCF/6-31G**	1.266	
$H_2Cl^+, ^1A_1$	$C_{2v}$	MP2(full)/6-31G**	1.268	
		MP2(full)/TZP	1.274	
		EXPT	1.275	
$H_3Cl^{2+}, ^1A_1$	$C_{3v}$	SCF/6-31G**	1.290	97.3
		MP2(full)/6-31G**	1.293	95.9
		MP2(full)/TZP	1.300	94.2
$H_3Cl^{2+}, ^1A_1'$	$C_{3v}$	SCF/6-31G**	1.348	100.7
		MP2(full)/6-31G**	1.353	95.8
		MP2(full)/TZP	1.365	98.4
$H_3Cl^{2+}, ^1A_1'$	$D_{3h}$	SCF/6-31G**	1.358	120.
		MP2(full)/6-31G**	1.360	120.
		MP2(full)/TZP	1.373	120.
		SCF/6-31G**	2.336 <sup>a</sup>	109.6 <sup>b</sup>
$H_3Cl^{2+}(ts), ^1A_1, C_s$	$C_s$		1.315 <sup>c</sup>	98.8 <sup>d</sup>
		MP2(full)/6-31G**	2.432 <sup>a</sup>	108.4 <sup>b</sup>
			1.319 <sup>c</sup>	97.4 <sup>d</sup>
		MP2(full)/TZP	2.471 <sup>a</sup>	108.8 <sup>b</sup>
			1.326 <sup>c</sup>	95.9 <sup>d</sup>
		SCF/6-31G**	1.493	109.47
$H_4Cl^{3+}, ^1A_1$	$T_d$	MP2(full)/6-31G**	1.500	109.47
		MP2(full)/TZP	1.521	109.47
		SCF/6-31G**	0.985	
$HNe^+, ^1\Sigma^+$	$C_{\infty v}$	MP2(full)/6-31G**	1.007	
$HAr^+, ^1\Sigma^+$	$C_{\infty v}$	SCF/6-31G**	1.267	
		MP2(full)/6-31G**	1.268	
		MP2(full)/TZP	1.278	
$H_2Ar^{2+}, ^1A_1$	$C_{2v}$	SCF/6-31G**	1.389	104.9
		MP2(full)/6-31G**	1.385	103.7
		MP2(full)/TZP	1.4051	102.5
$H_2Ar^{2+}(ts), ^1A'$	$C_s$	SCF/6-31G**	1.863 <sup>a</sup>	
			1.340 <sup>b</sup>	111.9 <sup>c</sup>
		MP2(full)/6-31G**	1.910 <sup>a</sup>	
			1.334 <sup>b</sup>	110.9 <sup>c</sup>
		MP2(full)/TZP	1.998 <sup>a</sup>	
	1.343 <sup>b</sup>	111.5 <sup>c</sup>		

<sup>a</sup>The distance between the central atom and the departing H atom labeled  $b$ .

<sup>b</sup>The distance between the central atom and the other H atoms labeled  $t$ .

<sup>c</sup>The angle  $H_bMH_r$ .

<sup>d</sup>The angle  $H_tMH_r$ .

<sup>e</sup>Data taken from M. W. Chase, Jr., C. A. Davies, J. R. Downey, Jr., D. J. Fouip, R. A. McDonald, A. N. Syverud, *JANAF Thermochemical Tables*, 3rd ed., J. Phys. Chem. Ref. Data 14 (1985), Suppl. 1.

$H_3S^+$ ,  $HF$ ,  $NeH^+$ ,  $ArH^+$ , and  $HCl$  as well as the dissociation energies of the  $H_3O^+$ ,  $H_3S^+$ ,  $H_2F^+$ ,  $HNe^+$ ,  $HAr^+$ , and  $H_2Cl^+$  cations are in good agreement ( $<3$  kcal/mol for the energies) with experimental data. We expect our results to be equally accurate for the doubly and triply charged species (for which experimental data are not available). Now, let us focus on each of the various classes of multiply protonated cations treated here, in each case con-

sidering the species' geometries, vibrational frequencies, intensities, and energetic stabilities.

#### A. $H_4O^{2+}$ and $H_4S^{2+}$

##### 1. Nature of the $H_4O^{2+} \rightarrow H_3O^+ + H^+$ energy surface

Both of the above dications have tetrahedral local-minimum structures as expected. The potential energy sur-

TABLE II. Calculated total energies  $E_{\text{TOT}}$  (a.u.) of the  $\text{OH}_n^{k+}$ ,  $\text{FH}_n^{k+}$ ,  $\text{NeH}_n^{k+}$ ,  $\text{SH}_n^{k+}$ ,  $\text{ClH}_n^{k+}$ , and  $\text{ArH}_n^{k+}$  cations.

Species	Symmetry	State	SCF/6-31G**	MP2(full)/6-31G**	MP2(full)/6-311G***
$\text{OH}_2$	$C_{2v}$	$^1A_1$	-76.023 62	-76.222 45	-76.287 13
$\text{OH}_3^+$	$C_{3v}$	$^1A_1$	-76.310 32	-76.508 97	-76.564 09
$\text{OH}_4^{2+}$	$T_d$	$^1A_1$	-76.220 63	-76.424 51	-76.479 91
$\text{OH}_4^{2+}$ (ts)	$C_{3v}$	$^1A_1$	-76.151 26	-76.355 28	-76.409 78
$\text{FH}$	$C_{\infty v}$	$^1\Sigma^+$	-100.011 69	-100.196 70	-100.289 15
$\text{FH}_2^+$	$C_{2v}$	$^1A_1$	-100.215 18	-100.404 30	-100.483 03
$\text{FH}_3^{2+}$	$D_{3h}$	$^1A_1'$	-100.041 87	-100.235 89	-100.313 12
$\text{FH}_3^{2+}$ (ts)	$C_{2v}$	$^1A_1$	-100.025 86	-100.219 33	-100.288 85
$\text{FH}_4^{3+}$	$T_d$	$^1A_1$	-99.580 64	-99.790 48	-99.864 40
Ne		$^1S$	-128.474 41	-128.626 18	
$\text{NeH}^+$	$C_{\infty v}$	$^1\Sigma^+$	-128.555 88	-128.716 72	
$\text{SH}_2$	$C_{2v}$	$^1A_1$	-398.675 03	-398.821 13	-398.967 13
$\text{SH}_3^+$	$C_{3v}$	$^1A_1$	-398.952 53	-399.102 97	-399.250 56
$\text{SH}_3^+$	$D_{3h}$	$^1A_1'$	-398.903 34	-399.054 00	-399.200 18
$\text{SH}_4^{2+}$	$T_d$	$^1A_1$	-398.914 48	-399.063 14	-399.212 69
$\text{SH}_4^{2+}$ (ts)	$C_{3v}$	$^1A_1$	-398.818 47	-398.969 60	-399.115 96
$\text{ClH}$	$C_{\infty v}$	$^1\Sigma^+$	-460.066 21	-460.215 62	-460.292 97
$\text{ClH}_2^+$	$C_{2v}$	$^1A_1$	-460.278 83	-460.436 39	-460.516 25
$\text{ClH}_3^{2+}$	$C_{3v}$	$^1A_1$	-460.175 37	-460.336 64	-460.420 09
$\text{ClH}_3^{2+}$	$D_{3h}$	$^1A_1'$	-460.147 15	-460.307 20	-460.389 36
$\text{ClH}_3^{2+}$ (ts)	$C_s$	$^1A'$	-460.128 69	-460.281 11	-460.360 03
$\text{ClH}_4^{3+}$	$T_d$	$^1A_1$	-459.791 47	-459.952 78	-460.041 98
$\text{ClH}_4^{3+}$ (ts <sub>1</sub> )	$C_{3v}$	$^1A_1$	-459.790 56	-459.951 85	-460.041 11
$\text{ClH}_4^{3+}$ (ts <sub>2</sub> )	$C_{2v}$	$^1A_1$	-459.786 51	-459.947 98	
Ar		$^1S$	-526.773 75	-526.919 99	-527.007 48
$\text{ArH}^+$	$C_{\infty v}$	$^1\Sigma^+$	-526.909 61	-527.066 87	-527.158 81
$\text{ArH}_2^{2+}$	$C_{2v}$	$^1A_1$	-526.719 41	-526.881 81	-526.978 68
$\text{ArH}_2^{2+}$ (ts)	$C_s$	$^1A'$	-526.709 34	-526.869 06	-526.964 68

\*For the  $\text{OH}_n^{k+}$  and  $\text{FH}_n^{k+}$  species, (10s6p1d/5s3p1) basis sets were used for O and F and a (5s1p/3s1p) basis set was used for H.

TABLE III. Calculated correlated energies (a.u.) of the  $\text{OH}_n^{k+}$ ,  $\text{FH}_n^{k+}$ ,  $\text{NeH}_n^{k+}$ ,  $\text{SH}_n^{k+}$ ,  $\text{ClH}_n^{k+}$ , and  $\text{ArH}_n^{k+}$  cations.

Species	Symmetry	State	MP2/6-311G (2df, 2p)	MP3/6-311G (2df, 2p)	MP4/6-311G (2df, 2p)	QCISD(T) /6-311G(2df, 2p)
Ne		$^1S$	-128.779 69	-128.781 49	-128.786 67	-128.786 27
$\text{NeH}^+$	$C_{\infty v}$	$^1\Sigma^+$	-128.867 65	-128.868 70	-128.875 72	-128.875 09
$\text{FH}$	$C_{\infty v}$	$^1\Sigma^+$	-100.314 45	-100.315 74	-100.324 22	-100.323 56
$\text{FH}_2^+$	$C_{2v}$	$^1A_1$	-100.514 36	-100.516 48	-100.525 22	-100.524 65
$\text{FH}_3^{2+}$	$D_{3h}$	$^1A_1'$	-100.340 82	-100.341 95	-100.351 12	-100.350 46
$\text{FH}_3^{2+}$ (ts)	$C_{2v}$	$^1A_1$	-100.319 16	-100.318 65	-100.329 16	-100.328 14
$\text{FH}_4^{3+}$	$T_d$	$^1A_1$	-99.891 56	-99.883 69	-99.899 56	-99.896 82
$\text{OH}_2$	$C_{2v}$	$^1A_1$	-76.305 22	-76.310 38	-76.319 83	-76.319 38
$\text{OH}_3^+$	$C_{3v}$	$^1A_1$	-76.584 99	-76.592 22	-76.600 74	-76.600 58
$\text{OH}_4^{2+}$	$T_d$	$^1A_1$	-76.495 99	-76.502 86	-76.511 70	-76.511 65
$\text{OH}_4^{2+}$ (ts)	$C_{3v}$	$^1A_1$	-76.429 45	-76.434 60	-76.444 48	-76.444 07
Ar		$^1S$	-526.976 42	-526.990 34	-526.992 66	-526.992 77
$\text{ArH}^+$	$C_{\infty v}$	$^1\Sigma^+$	-527.122 23	-527.138 45	-527.142 33	-527.142 78
$\text{ArH}_2^{2+}$	$C_{2v}$	$^1A_1$	-526.940 35	-526.957 21	-526.961 86	-526.962 59
$\text{ArH}_2^{2+}$ (ts)	$C_s$	$^1A'$	-526.930 71	-526.946 45	-526.950 75	-526.951 30
$\text{ClH}$	$C_{\infty v}$	$^1\Sigma^+$	-460.293 74	-460.314 18	-460.320 86	-460.321 34
$\text{ClH}_2^+$	$C_{2v}$	$^1A_1$	-460.510 43	-460.532 97	-460.540 28	-460.541 13
$\text{ClH}_3^{2+}$	$C_{3v}$	$^1A_1$	-460.409 81	-460.433 14	-460.440 77	-460.441 93
$\text{ClH}_3^{2+}$	$D_{3h}$	$^1A_1'$	-460.378 10	-460.401 09	-460.408 36	-460.409 28
$\text{ClH}_3^{2+}$ (ts)	$C_s$	$^1A'$	-460.355 06	-460.376 67	-460.384 32	-460.385 11
$\text{ClH}_4^{3+}$	$T_d$	$^1A_1$	-460.027 93	-460.050 28	-460.057 87	-460.058 90
$\text{ClH}_4^{3+}$ (ts <sub>1</sub> )	$C_{3v}$	$^1A_1$	-460.028 08	-460.050 26	-460.057 85	-460.058 85
$\text{SH}_2$	$C_{2v}$	$^1A_1$	-398.888 74	-398.911 71	-398.919 44	-398.920 43
$\text{SH}_3^+$	$C_{3v}$	$^1A_1$	-399.165 07	-399.189 80	-399.197 83	-399.199 36
$\text{SH}_3^+$	$D_{3h}$	$^1A_1'$	-399.115 62	-399.139 97	-399.147 54	-399.148 74
$\text{SH}_4^{2+}$	$T_d$	$^1A_1$	-399.029 34	-399.052 91	-399.061 09	-399.062 39
$\text{SH}_4^{2+}$ (ts)	$C_{3v}$	$^1A_1$	-398.995 25	-399.015 26	399.021 74	-399.023 15

\*Total energies of the  $\text{NeH}^+$  cation calculated at the MP2(full)/6-31G\*\* geometry. For Ar,  $\text{ArH}^+$ , and  $\text{ArH}_2^{2+}$  a 311G(2d,2p) basis set was employed.

TABLE IV. Calculated dissociation energies ( $E_{\text{diss}}$ ) and dissociation barriers ( $E^+$ ) (kcal/mol) at MP2(full)/6-311G\*\* geometries With the 6-311G(2df,2p)<sup>a</sup> basis sets.

Reaction	MP2		MP3		MP4		QCISD(T)		QCISD(T)+ZPE <sup>b</sup>	
	$E_{\text{diss}}$	$E^+$	$E_{\text{diss}}$	$E^+$	$E_{\text{diss}}$	$E^+$	$E_{\text{diss}}$	$E^+$	$E_{\text{diss}}$	$E^+$
1. OH <sub>3</sub> <sup>+</sup> -OH <sub>2</sub> +H <sup>+</sup>	+175.6	...	+176.9	...	+176.3	...	+176.5	...	+168.0	...
2. OH <sub>4</sub> <sup>2+</sup> -OH <sub>2</sub> +2H <sup>+</sup>	+119.7	...	+120.8	...	+120.4	...	+120.7	...	+106.7	...
3. OH <sub>4</sub> <sup>2+</sup> -OH <sub>3</sub> <sup>+</sup> +H <sup>+</sup>	-55.8	41.8	-56.1	42.8	-55.9	42.2	-55.8	42.4	-61.3	38.1
4. FH <sub>2</sub> <sup>+</sup> -FH+H <sup>+</sup>	+125.4	...	+126.0	...	+126.1	...	+126.2	...	+120.0	...
5. FH <sub>3</sub> <sup>2+</sup> -FH+2H <sup>+</sup>	+16.5	...	+16.4	...	+16.9	...	+16.9	...	+8.9	...
6. FH <sub>3</sub> <sup>2+</sup> -FH <sub>2</sub> <sup>+</sup> +H <sup>+</sup>	-108.9	13.6	-109.5	14.6	-109.2	13.8	-109.3	14.0	-111.1	12.2
7. FH <sub>4</sub> <sup>3+</sup> -FH+3H <sup>+</sup>	-265.4	...	-271.1	...	-266.5	...	-267.8	...	-270.8	...
8. FH <sub>4</sub> <sup>3+</sup> -FH <sub>2</sub> <sup>+</sup> +2H <sup>+</sup>	-390.8	...	-397.1	...	-392.6	...	-394.0	...	-390.8	...
9. FH <sub>4</sub> <sup>3+</sup> -FH <sub>3</sub> <sup>2+</sup> +H <sup>+</sup>	-281.9	...	-287.6	...	-283.4	...	-284.7	...	-279.7	...
10. NeH <sup>+</sup> -Ne+H <sup>+</sup>	+55.2	...	+54.7	...	+55.9	...	+55.7	...	+51.7	...
11. SH <sub>3</sub> <sup>+</sup> -SH <sub>2</sub> +H <sup>+</sup>	+173.4	...	+174.5	...	+174.7	...	+175.0	...	+167.8	...
12. SH <sub>2</sub> <sup>+</sup> -SH <sub>2</sub> +2H <sup>+</sup>	+88.2	...	+88.6	...	+88.9	...	+89.1	...	+76.4	...
13. SH <sub>2</sub> <sup>+</sup> -SH <sub>3</sub> <sup>+</sup> +H <sup>+</sup>	-85.2	21.4	-85.9	23.6	-85.8	24.7	-85.9	24.6	-91.4	19.7
14. ClH <sub>2</sub> <sup>+</sup> -ClH+H <sup>+</sup>	+136.0	...	+137.3	...	+137.7	...	+137.9	...	+132.2	...
15. ClH <sub>3</sub> <sup>2+</sup> -ClH+2H <sup>+</sup>	+72.8	...	+74.6	...	+75.2	...	+75.7	...	+65.0	...
16. ClH <sub>3</sub> <sup>2+</sup> -ClH <sub>2</sub> <sup>+</sup> +H <sup>+</sup>	-63.1	34.4	-62.6	35.4	-62.4	35.4	-62.2	35.7	-67.2	33.8
17. ClH <sub>4</sub> <sup>3+</sup> -ClH+3H <sup>+</sup>	-166.8	...	-165.6	...	-165.0	...	-164.7	...	-173.7	...
18. ClH <sub>4</sub> <sup>3+</sup> -ClH <sub>2</sub> <sup>+</sup> +2H <sup>+</sup>	-302.8	...	-302.9	...	-302.7	...	-302.6	...	-305.9	...
19. ClH <sub>4</sub> <sup>3+</sup> -ClH <sub>3</sub> <sup>2+</sup> +H <sup>+</sup>	-239.6	-0.1	-240.2	0.0	-240.3	0.0	-240.4	0.0	-242.9	0.0
20. ArH <sup>+</sup> -Ar+H	+91.5	...	+92.9	...	+93.9	...	+94.1	...	+90.0	...
21. ArH <sub>2</sub> <sup>2+</sup> -Ar+2H <sup>+</sup>	-22.6	...	-20.8	...	-19.3	...	-18.9	...	-25.7	...
22. ArH <sub>2</sub> <sup>2+</sup> -ArH <sup>+</sup> +H <sup>+</sup>	-114.1	6.0	-113.7	6.8	-113.2	7.0	-113.1	7.1	-115.8	4.6

<sup>a</sup>The argon containing species were calculated with a 6-311G(2d,2p) basis set.<sup>b</sup>Zero-point corrected.TABLE V. (a) Calculated frequencies (cm<sup>-1</sup>) and ir (KM/mol) and Raman (Å<sup>4</sup>/amu) intensities of OH<sub>n</sub><sup>k+</sup> species. (b) Calculated frequencies (cm<sup>-1</sup>) and ir (KM/mol) and Raman (Å<sup>4</sup>/amu) intensities of FH<sub>n</sub><sup>k+</sup> and NeH<sup>+</sup> species. (c) Calculated frequencies (cm<sup>-1</sup>) and ir (KM/mol) and Raman (Å<sup>4</sup>/amu) intensities of SH<sub>n</sub><sup>k+</sup> species. (d) Calculated frequencies (cm<sup>-1</sup>) and ir (KM/mol) and Raman (Å<sup>4</sup>/amu) intensities of ClH<sub>n</sub><sup>k+</sup> and ArH<sub>n</sub><sup>k+</sup> species.

(a)	Species	Symmetry	State	SCF/6-31G**		MP2(full)/6-31G**		Exptl.	Freq. <sup>a</sup>
				Freq.	ir	Ram.	Freq.		
	OH <sub>2</sub>	C <sub>2v</sub>	<sup>1</sup> A <sub>1</sub>	ν <sub>1</sub> (a <sub>1</sub> ) = 4147	16	75	3895	4	3656.65
				ν <sub>2</sub> (a <sub>1</sub> ) = 1770	105	6	1683	78	1594.78
				ν <sub>3</sub> (b <sub>2</sub> ) = 4264	58	37	4033	34	3755.79
				ZPE=14.6			13.7		
	OH <sub>3</sub> <sup>+</sup>	C <sub>3v</sub>	<sup>1</sup> A <sub>1</sub>	ν <sub>1</sub> (a <sub>1</sub> ) = 3857	46	39	3644	47	
				ν <sub>2</sub> (a <sub>1</sub> ) = 782	629	1	867	547	
				ν <sub>3</sub> (e) = 3993	630	11	3785	522	
				ν <sub>4</sub> (e) = 1789	141	2	1712	121	
				ZPE=23.2			22.2		
	OH <sub>4</sub> <sup>2+</sup>	T <sub>d</sub>	<sup>1</sup> A <sub>1</sub>	ν <sub>1</sub> (a <sub>1</sub> ) = 3175	0	30	2967	0	
				ν <sub>2</sub> (e) = 1702	0	3	1631	0	
				ν <sub>3</sub> (t <sub>2</sub> ) = 3069	1164	7	2893	1049	
				ν <sub>4</sub> (t <sub>2</sub> ) = 1569	438	1	1480	414	
				ZPE=29.3			27.7		
	OH <sub>4</sub> <sup>2+</sup> (ts)	C <sub>3v</sub>	<sup>1</sup> A <sub>1</sub>	ν <sub>1</sub> (a <sub>1</sub> ) = 3576			3355		
				ν <sub>2</sub> (a <sub>1</sub> ) = 1421			1341		
				ν <sub>3</sub> (a <sub>1</sub> ) = 872i			837i		
				ν <sub>4</sub> (e) = 3615			3423		
				ν <sub>5</sub> (e) = 1773			1688		
				ν <sub>6</sub> (e) = 787			732		
				ZPE=24.8			23.4		
(b)	FH	C <sub>∞v</sub>	<sup>1</sup> Σ <sup>+</sup>	ωe=4493	133	30	4193	82	4141.03
				ZPE=6.4			6.0		
	FH <sub>2</sub> <sup>+</sup>	C <sub>2v</sub>	<sup>1</sup> A <sub>1</sub>	ν <sub>1</sub> (a <sub>1</sub> ) = 3796	290	18	3539	242	
				ν <sub>2</sub> (a <sub>1</sub> ) = 1481	329	1	1453	287	
				ν <sub>3</sub> (b <sub>2</sub> ) = 3800	1062	5	3569	881	
				ZPE=13.0			12.2		

TABLE V. (Continued.)

(b)	Species	Symmetry	State	SCF/6-31G**		MP2(full)/6-31G**			Exptl. Freq. <sup>a</sup>
				Freq.	ir	Ram.	Freq.	ir	
	FH <sub>3</sub> <sup>2+</sup>	D <sub>3h</sub>	<sup>1</sup> A <sub>1</sub> '	$\nu_1(a_1') = 2615$	0	13	2757	0	
				$\nu_2(a_2'') = 574$	1175	0	396	1140	
				$\nu_3(e') = 2253$	2183	1	2140	2064	
				$\nu_4(e') = 1406$	172	1	1330	159	
				ZPE=15.0			14.0		
	FH <sub>3</sub> <sup>2+</sup> (ts)	C <sub>2v</sub>	<sup>1</sup> A <sub>1</sub>	$\nu_1(a_1) = 3105$			2917		
				$\nu_2(a_1) = 1550$			1485		
				$\nu_3(a_1) = 1069i$			1031i		
				$\nu_4(b_1) = 587$			462		
				$\nu_5(b_2) = 2981$			2829		
				$\nu_6(b_2) = 906$			849		
				ZPE=13.1			12.2		
	FH <sub>4</sub> <sup>3+</sup>	T <sub>d</sub>	<sup>1</sup> A <sub>1</sub>	$\nu_1(a_1) = 1210$			1181		
				$\nu_2(e) = 993$			977		
				$\nu_3(t_2) = 1102$			1043		
				$\nu_4(t_2) = 1396i$			1266i		
				ZPE=9.3			9.0		
	NeH <sup>+</sup>	C <sub>∞v</sub>	<sup>1</sup> Σ <sup>+</sup>	$\nu = 2884$			2805		
				ZPE=4.1			4.0		
(c)	Species	Symmetry	State	SCF/6-31G**		MP2(full)/6-31G**			Exptl. Freq. <sup>a</sup>
				Freq.	ir	Ram.	Freq.	ir	
	SH <sub>2</sub>	C <sub>2v</sub>	<sup>1</sup> A <sub>1</sub>	$\nu_1(a_1) = 2897$	4	178	2847	4	2614.56
				$\nu_2(a_1) = 1341$	7	44	1270	8	1182.68
				$\nu_3(b_2) = 2909$	8	134	2874	7	2625
				ZPE=10.2			10.0		
	SH <sub>3</sub> <sup>+</sup>	C <sub>3v</sub>	<sup>1</sup> A <sub>1</sub>	$\nu_1(a_1) = 2850$	50	158	2777	48	
				$\nu_2(a_1) = 1169$	12	12	1119	11	
				$\nu_3(e) = 2860$	79	87	2800	74	
				$\nu_4(e) = 1367$	0	31	1283	0	
	SH <sub>3</sub> <sup>+</sup>	D <sub>3h</sub>	<sup>1</sup> A <sub>1</sub> '	$\nu_1(a_1) = 2870$			2827		
				$\nu_2(a_2'') = 1191i$			1139i		
				$\nu_3(e') = 2965$			2928		
				$\nu_4(e') = 1206$			1143		
	SH <sub>4</sub> <sup>2+</sup>	T <sub>d</sub>	<sup>1</sup> A <sub>1</sub>	$\nu_1(a_1) = 2631$	0	168	2557	0	
				$\nu_2(e) = 1315$	0	22	1243	0	
				$\nu_3(t_2) = 2640$	596	39	2574	587	
				$\nu_4(t_2) = 1101$	24	6	1026	31	
	SH <sub>4</sub> <sup>2+</sup> (ts)	C <sub>3v</sub>	<sup>1</sup> A <sub>1</sub>	ZPE=23.6			15.7		
				$\nu_1(a_1) = 2759$			2687		
				$\nu_2(a_1) = 1098$			1049		
				$\nu_3(a_1) = 715i$			716i		
	SH <sub>4</sub> <sup>2+</sup> (ts)	C <sub>3v</sub>	<sup>1</sup> A <sub>1</sub>	$\nu_4(e) = 2772$			2710		
				$\nu_5(e) = 1315$			1240		
				$\nu_6(e) = 429$			402		
				ZPE=1-8.4			17.8		
(d)	Species	Symmetry	State	SCF/6-31G**		MP2(full)/6-31G**			Exptl. Freq. <sup>a</sup>
				Freq.	ir	Ram.	Freq.	ir	
	ClH	C <sub>∞v</sub>	<sup>1</sup> Σ <sup>+</sup>	$\omega_e = 3180$	34	117	3125	22	2990.94
				ZPE=4.5			4.5		
	ClH <sub>2</sub> <sup>+</sup>	C <sub>2v</sub>	<sup>1</sup> A <sub>1</sub>	$\nu_1(a_1) = 2967$	233	96	2909	197	
				$\nu_2(a_1) = 1351$	21	19	1277	18	
				$\nu_3(b_2) = 2962$	362	57	2916	300	
				ZPE=10.4			10.2		
	ClH <sub>3</sub> <sup>2+</sup>	C <sub>3v</sub>	<sup>1</sup> A <sub>1</sub>	$\nu_1(a_1) = 2509$	409	87	2453	372	
				$\nu_2(a_1) = 1035$	192	7	1009	178	
				$\nu_3(e) = 2410$	1003	34	2367	880	
				$\nu_4(e) = 1286$	28	15	1220	28	
				ZPE=15.6			15.2		
	ClH <sub>3</sub> <sup>2+</sup>	D <sub>3h</sub>	<sup>1</sup> A <sub>1</sub> '	$\nu_1(a_1') = 2365$			2347		
				$\nu_2(a_2'') = 925i$			915i		
				$\nu_3(e') = 2313$			2306		

TABLE V. (Continued.)

(d)	Species	Symmetry	State	SCF/6-31G**		MP2(full)/6-31G**		Exptl. Freq. <sup>a</sup>
				Freq.	ir	Ram.	Freq.	
				$\nu_4(e') = 1088$			1035	
				ZPE=13.1			12.9	
	$\text{CH}_3^+(\text{ts})$	$C_s$	$^1A'$	$\nu_1(a') = 2735$			2683	
				$\nu_2(a') = 1302$			1237	
				$\nu_3(a') = 554$			523	
				$\nu_4(a') = 841i$			817i	
				$\nu_5(a'') = 2713$			2675	
				$\nu_6(a'') = 616$			588	
				ZPE=11.3			11.0	
	$\text{CH}_4^+$	$T_d$	$^1A_1$	$\nu_1(a_1) = 1612$	0	90	1591	0
				$\nu_2(e) = 1062$	0	17	1012	0
				$\nu_3(t_2) = 1237$	2673	7	1220	2531
				$\nu_4(t_2) = 764$	14	11	727	2
				ZPE=13.9			13.5	
	$\text{CH}_4^+(\text{ts}_1)$	$C_{3v}$	$^1A_1$	$\nu_1(a_1) = 1713$			1691	
				$\nu_2(a_1) = 950$			907	
				$\nu_3(a_1) = 895i$			888i	
				$\nu_4(e) = 1441$			1426	
				$\nu_5(e) = 1062$			1012	
				$\nu_6(e) = 750$			712	
				ZPE=13.1			12.7	
	$\text{CH}_4^+(\text{ts}_2)$	$C_{2v}$	$^1A_1$	$\nu_1(a_1) = 1965$			1947	
				$\nu_2(a_1) = 1125$			1074	
				$\nu_3(a_1) = 671$			639	
				$\nu_4(a_1) = 857i$			844i	
				$\nu_5(a_2) = 936$			896	
				$\nu_6(b_1) = 1837$			1828	
				$\nu_7(b_1) = 697$			666	
				$\nu_8(b_2) = 874$			837	
				$\nu_9(b_2) = 1243i$			1244i	
				ZPE=11.6			11.3	
	$\text{ArH}^+$	$C_{\infty v}$	$^1\Sigma^+$	$\nu = 2896$	680	43	2884	567
				ZPE=4.1			4.1	
	$\text{ArH}_2^+$	$C_{2v}$	$^1A_1$	$\nu_1(a_1) = 1953$	1003	34	1989	882
				$\nu_2(a_1) = 1040$	127	9	1024	128
				$\nu_3(b_2) = 1699$	1976	13	1766	1747
				ZPE=6.7			6.8	
	$\text{ArH}_2^+(\text{ts})$	$C_s$	$^1A'$	$\nu_1(a') = 2230$			2282	
				$\nu_2(a') = 736$			710	
				$\nu_3(a') = 1041i$			1033i	
				ZPE=4.2			4.3	

<sup>a</sup>Data from M. W. Chase, Jr., C. A. Davies, J. R. Downey, Jr., D. J. Fouip, R. A. McDonald, A. N. Syverud, *JANAF Thermochemical Tables*, 3rd ed. J. Phys. Chem. Ref. Data **14** (1985), Suppl. 1.

faces (see Fig. 1 for that of the oxygen-containing dication) for  $\text{H}_4\text{O}^{2+}$  and  $\text{H}_4\text{S}^{2+}$  are repulsive at large  $\text{H}_3\text{X}^+-\text{H}^+$  separation due to the large Coulomb repulsion between the two unit positive charges. Near the barrier, electron density from the  $\text{H}_3\text{X}^+$  moiety flows to the approaching  $\text{H}^+$  ion, as the fourth X-H  $\sigma$  bond begins to form. This flow in density is monitored in Fig. 1 through the partial charges on the approaching ( $\text{H}_b$ ) and three equivalent ( $\text{H}_c$ ) hydrogen atom centers. Once this new bond is formed, the entire +2 charge is distributed through all *four* H atom centers as a result of which the quantum mechanical Coulomb repulsion energy is dramatically reduced. At the tetrahedral geometry, the charge delocalization is optimal and entirely uniform, and the total energy is a minimum.

## 2. Comparison with classical Coulomb electrostatic energies

It is informative to examine the nature of the Coulombic energy content of these species in further detail, and, in particular, to compare the results of our quantum calculations to predictions of various classical electrostatic models. So doing can increase our understanding of the forces that act to stabilize these species.

In Fig. 1 we display our fully quantal  $\text{H}_4\text{O}^{2+}$  energies as functions of the distance  $R(\text{OH})$  between the O atom and the unique  $\text{H}^+$  cation [with the other internal geometrical degrees of freedom optimized for each such  $R(\text{OH})$ ]. Also shown are the corresponding energies (at these same nuclear geometries) of a classical model that intentionally excludes bond formation with the approaching  $\text{H}^+$  ion.

The higher energy curve in Fig. 1 gives the energy of interaction of a unit positive charge located on the unique H center with an  $\text{H}_3\text{O}^+$  ion whose internal geometry is made identical to that obtained in our *ab initio*  $\text{H}_4\text{O}^{2+}$  calculations at each  $R(\text{OH})$ , but whose orbitals have been SCF-optimized in the presence of the unit positive charge on the unique H center. In these calculations, the net charges on the three identical H atoms and the O atom reflect the quantal charge distribution of  $\text{H}_3\text{O}^+$  polarized by the unit positive charge at  $R(\text{OH})$ . Although these energies closely parallel the correct  $\text{H}_4\text{O}^{2+}$  energies down to  $\sim 2.1$  Å, they deviate strongly for shorter distances. In particular, as the fourth O–H bond begins to form, the  $\text{H}_4\text{O}^{2+}$  quantum energy (which contains an attractive O–H bond energy contribution that both classical curves are lacking) drops significantly below this energy. For example, at the  $\text{H}_4\text{O}^{2+}$  equilibrium geometry, the quantum energy is 56 kcal/mol above the  $\text{H}_3\text{O}^+ + \text{H}^+$  asymptote whereas this model's energy lies at 112 kcal/mol.

Another difference between the fully quantal results and those of the classical Coulomb interaction model outlined above resides in the symmetry of the charge distribution in the former that is absent in the latter. Specifically, our quantal results show four equally charged H atoms, but in the above model, the classical Coulomb energy was calculated for a "charge localized" state. To further investigate the effects of charge delocalization, one can compute (e.g., at  $R(\text{OH}) = 1.0228$  Å where all four O–H distances are equal) the Coulombic energy content of a unit positive charge on one H center with three  $+1/3$  charges on the

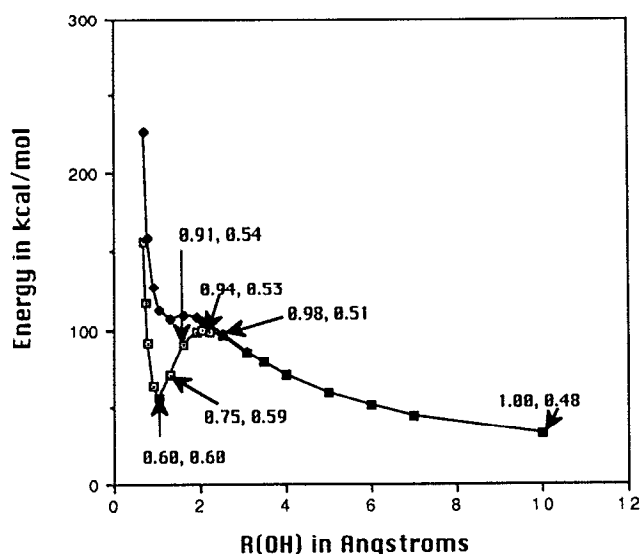


FIG. 1. The lowest energy curve gives a plot of the SCF/6-31G\*\* ground state electronic energy (including nuclear repulsion) of  $\text{H}_4\text{O}^{2+}$  as a function of one O–H bond length  $R(\text{OH})$  with the remaining internal coordinates of the  $\text{H}_3\text{O}^+$  moiety optimized to produce minimum energy for each value of  $R(\text{OH})$ . The partial charges on the departing H atom and those on the three remaining H atoms are given by the pairs of numbers (e.g., 0.94 and 0.53 are the charges near the barrier top). The higher energy curve represents the interaction energy of a single unit positive charge on the unique H atom center at  $R(\text{OH})$  interacting with  $\text{H}_3\text{O}^+$ . The two curves are close or indistinguishable for  $R(\text{OH}) > \sim 2.1$  Å.

other three H centers compared to the Coulomb energy of four equal  $+1/2$  charges on the four H centers. The former lies 196 kcal/mol above the  $\text{H}_3\text{O}^+ + \text{H}^+$  asymptote, and the latter lies even 33 kcal/mol higher.

It may be surprising that four equivalent charges of magnitude  $1/2$  produce greater classical Coulombic repulsion energy than the charge localized state with one unit charge and three charges of magnitude  $1/3$ . At first glance, this aspect of the classical model seems inconsistent with the results of our quantum calculations which show equal charge densities (i.e., average charges) on the four equivalent H atoms. To achieve any sense of agreement, one can postulate that four equally weighted classical "resonance structures" (each with one of the H atoms carrying  $\sim$  unit charge and the remaining three having charge  $\sim 1/3$ ) are superposed to produce the quantum state and that the classical picture corresponds to only one of these resonance structures. The difference between the quantum and classical results is then ascribed to quantum interferences among the four structures.

### 3. High energy content of multiprotonated species

Of course, the  $T_d$   $\text{H}_4\text{O}^{2+}$  and  $\text{H}_4\text{S}^{2+}$  structures are not the lowest-energy geometries that these species can realize. The dissociation products  $\text{H}_3\text{X}^+$  and  $\text{H}^+$  are predicted to be lower in energy by 61 and 91 kcal/mol, respectively, at the QCISD(T)/6-311(2df,2p)//MP2(full)/TZP+ZPE/MP2(full)/6-31G\*\* level for these two dications. These  $T_d$  forms of  $\text{H}_4\text{O}^{2+}$  and  $\text{H}_4\text{S}^{2+}$  are separated from their dissociation products by barriers of 38 and 20 kcal/mol, as a result of which both of them may be sufficiently long lived to be detected in gas-phase experiments.

### B. $\text{H}_3\text{F}^{2+}$ and $\text{H}_3\text{Cl}^{2+}$

$C_{3v}$  pyramidal structures with one lone electron pair on the central atom are expected (in analogy<sup>14,15</sup> with  $\text{NH}_3$  and  $\text{H}_3\text{O}^+$ ) for  $\text{H}_3\text{F}^{2+}$  and  $\text{H}_3\text{Cl}^{2+}$ . Both of these dications are found to have such local minima, but  $\text{H}_3\text{F}^{2+}$  actually has a  $D_{3h}$  planar structure (because the Coulomb repulsions between its hydrogen atoms are larger than in  $\text{ClH}_3^{2+}$ , which is found to have a pyramidal  $C_{3v}$  structure). At our highest QCISD(T)/6-311G(2df,2p)/MP2(full)/TZP+ZPE/MP2(full)/6-31G\*\* level, the  $\text{H}_3\text{Cl}^{2+}$  dication has a high (18 kcal/mol) inversion barrier. However, this value is much lower than inversion barriers of the isoelectronic  $\text{PH}_3$  [35 kcal/mol (Ref. 16)] and  $\text{SH}_3^+$  [32 kcal/mol (Ref. 17)] species, again due to the larger Coulomb repulsion among the hydrogen centers of  $\text{ClH}_3^{2+}$ .

The  $\text{H}_3\text{F}^{2+}$  and  $\text{H}_3\text{Cl}^{2+}$  dications are predicted to lie above their dissociation products ( $\text{H}_2\text{X}^+$  and  $\text{H}^+$ ) by 111 and 67 kcal/mol, respectively, at the QCISD(T)/6-311G(2df,2p)/MP2(full)/TZP+ZPE/MP2(full)/6-31G\*\* level. At this same level, our calculations indicate that  $\text{H}_3\text{F}^{2+}$  and  $\text{H}_3\text{Cl}^{2+}$  have 12 and 34 kcal/mol dissociation potential barriers, respectively.



### C. $\text{H}_2\text{Ne}^{2+}$ and $\text{H}_2\text{Ar}^{2+}$

For  $\text{H}_2\text{Ne}^{2+}$ , geometry optimization within  $D_{\infty h}$  or  $C_{2v}$  symmetry leads to dissociation into  $\text{H}^+ + \text{Ne} + \text{H}^+$ . Hence, this dication has no local minimum on its ground-state potential energy surface. In contrast, the  $\text{H}_2\text{Ar}^{2+}$  dication is found to possess a local minimum which lies 116 kcal/mol above  $\text{HAr}^+$  and  $\text{H}^+$ . However, this  $\text{H}_2\text{Ar}^{2+}$  structure is separated by a small barrier 5 kcal/mol from its dissociation products [all of this data refers to the QCISD(T)/6-311G(2d,2p)//MP2(full)/TZP+ZPE/MP2(full)/6-31G\*\* treatment), and thus may have a short life time.

### D. $\text{H}_4\text{F}^{3+}$ and $\text{H}_4\text{Cl}^{3+}$

Both  $\text{H}_4\text{F}^{3+}$  and  $\text{H}_4\text{Cl}^{3+}$  are expected to have tetrahedral structures. However,  $\text{H}_4\text{F}^{3+}$  is found to possess three imaginary vibrational frequencies in  $T_d$  symmetry and to not possess a local minimum on its ground state potential energy surface. In contrast,  $\text{H}_4\text{Cl}^{3+}$  has a local minimum with no imaginary frequencies at tetrahedral symmetry, but the corresponding potential barrier on the dissociation pathway is very small and is exceeded by the ZPE correction. Therefore, both of these trications are predicted to be unstable. The fact that  $\text{H}_4\text{Cl}^{3+}$  is nearly stable suggests that  $\text{H}_4\text{I}^{3+}$  may be stable since the larger I atom should delocalize the 3+ charges over larger H-to-H distances.

### E. $\text{H}_3\text{Ne}^{3+}$ and $\text{H}_3\text{Ar}^{3+}$

For both of these species, geometry optimization within  $C_{3v}$  or  $D_{3h}$  symmetry [at the SCF/6-31G\*\* and MP2(full)/6-31G\*\* levels] leads to dissociation into Ne (or Ar) +  $3\text{H}^+$  without any barrier, as a result of which both of these species are not viable.

### F. $\text{H}_4\text{Ne}^{4+}$ and $\text{H}_4\text{Ar}^{4+}$

These species also have no local minima on their respective potential energy surfaces because geometry optimization in  $T_d$  symmetry [at the SCF/6-31G\*\* and MP2(full)/6-31G\*\* levels] leads to dissociation into Ne (or Ar) +  $4\text{H}^+$  without any barrier.

### G. Energy content of the dications and mechanisms for its release

The multiply protonated cations studied in this paper possess a great deal of pent up energy as shown clearly in Fig. 1 and Table IV. If the barrier to dissociation can be surmounted (e.g., thermally), this energy may be released. The amount of energy released in such events is given as  $E_{\text{diss}}$  in Table IV, and ranges from  $\sim 60$  kcal/mol to greater than 110 kcal/mol.

Alternatively, energy release can be achieved by reducing the parent species' charge state by one unit (e.g., electrochemically or by photoinduced electron transfer from a neighboring moiety). For example, as illustrated in Fig. 2, addition of a single electron to  $\text{H}_4\text{O}^{2+}$  to form  $\text{H}_4\text{O}^+$  at the equilibrium geometry of the dication produces a very unstable situation. The nascent reduced species, which as Ta-

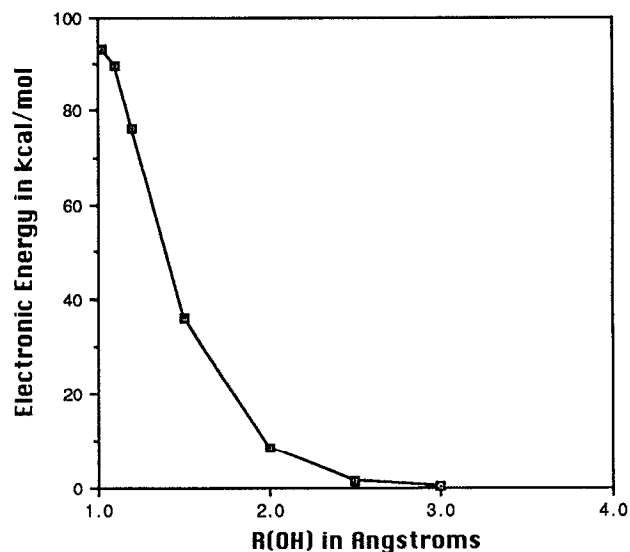


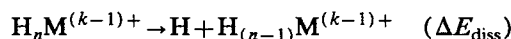
FIG. 2. Plot of the SCF/6-31G\*\* ground state electronic energy (including nuclear repulsion) of  $\text{H}_4\text{O}^+$  as a function of *one* O-H bond length  $R(\text{OH})$  with the remaining internal coordinates of the  $\text{H}_3\text{O}$  moiety optimized to produce minimum energy for each value of  $R(\text{OH})$ . Note that the geometry corresponding to  $R(\text{OH}) = 1.0228$  Å corresponds to the  $\text{H}_4\text{O}^+$  that would be formed by attaching an electron to  $\text{H}_4\text{O}^{2+}$  at its equilibrium geometry.

ble VI shows vertically lies  $\sim 13$  eV below the  $\text{H}_4\text{O}^{2+}$  dication, spontaneously dissociates to form  $\text{H} + \text{H}_3\text{O}^+$  with a very large release of kinetic energy (over 90 kcal/mol of energy in the  $\text{H}_4\text{O}^+$  case—see Fig. 2).

The energy releases corresponding to the doubly charged cations studied here are detailed quantitatively in Tables IV and VI. In the former, energy differences appropriate to tunneling through or surmounting the barrier on the parent ion surface are given as  $E_{\text{diss}}$ . In the latter, the adiabatic energy differences, denoted  $\Delta E_{\text{ad}}$ , combine the *electronic* energy gained by simply adding an electron to the parent species' at its equilibrium geometry (i.e., the vertical energy difference denoted  $\Delta E_v$  in this table)



and the subsequent kinetic energy released



when the reduced species explodes. The explosion energies

$$\Delta E_{\text{diss}} = |\Delta E_{\text{ad}} - \Delta E_v|$$

inferred from the data of Table VI lie between 2.8 and 3.4 eV, or 64 and 78 kcal/mol. We note that the vertical attachment energies  $\Delta E_v$  of the dications listed are in line with those of  $\text{Be}^{2+}$ ,  $\text{Mg}^{2+}$ ,  $\text{Al}^{2+}$ ,  $\text{Ni}^{2+}$ ,  $\text{Cu}^{2+}$ , and  $\text{Zn}^{2+}$ , which range from  $-15$  to  $-20$  eV.

## IV. CONCLUSIONS

(1) The *doubly charged*  $\text{H}_4\text{O}^{2+}$ ,  $\text{H}_4\text{S}^{2+}$ ,  $\text{H}_3\text{F}^{2+}$ ,  $\text{H}_3\text{Cl}^{2+}$ , and  $\text{H}_2\text{Ar}^{2+}$  cations are predicted to be metastable species that are not stable thermodynamically with re-

TABLE VI. Vertical ( $\Delta E_v$ ) and adiabatic ( $\Delta E_{ad}$ ) electron attachment energies in eV for doubly protonated species [within the 6-3111G(2df,2p) basis].<sup>a,b</sup>

Reaction	SCF	PMP2	PMP3	PMP4
$\Delta E_v$ $\text{H}_4\text{O}^{2+} + e \rightarrow \text{H}_4\text{O}^+$	12.4	13.1	13.1	13.2
$\Delta E_{ad}$ $\text{H}_4\text{O}^{2+} + e \rightarrow \text{H}_3\text{O}^+ + \text{H}$	16.1	16.0	16.0	16.0
$\Delta E_v$ $\text{H}_4\text{S}^{2+} + e \rightarrow \text{H}_4\text{S}^+$	13.2	13.9	13.9	14.0
$\Delta E_{ad}$ $\text{H}_4\text{S}^{2+} + e \rightarrow \text{H}_3\text{S}^+ + \text{H}$	17.3	17.3	17.3	17.3
$\Delta E_v$ $\text{H}_3\text{F}^{2+} + e \rightarrow \text{H}_3\text{F}^+$	14.7	15.4	15.4	15.4
$\Delta E_{ad}$ $\text{H}_3\text{F}^{2+} + e \rightarrow \text{H}_2\text{F}^+ + \text{H}$	18.4	18.3	18.4	18.3
$\Delta E_v$ $\text{H}_3\text{Cl}^{2+} + e \rightarrow \text{H}_3\text{Cl}^+$	12.9	13.3	13.3	13.3
$\Delta E_{ad}$ $\text{H}_3\text{Cl}^{2+} + e \rightarrow \text{H}_2\text{Cl}^+ + \text{H}$	16.3	16.3	16.3	16.3
$\Delta E_v$ $\text{H}_2\text{Ar}^{2+} + e \rightarrow \text{H}_2\text{Ar}^+$	14.7	15.1	15.1	15.1
$\Delta E_{ad}$ $\text{H}_2\text{Ar}^{2+} + e \rightarrow \text{HAr}^+ + \text{H}$	18.6	18.6	18.5	18.5

<sup>a</sup>The vertical  $\Delta E_v$  gives  $\Delta E$  (ZPE corrected) for the process  $\text{H}_n\text{M}^{k+} + e \rightarrow \text{H}_n\text{M}^{(k-1)+}$  at the geometry of  $\text{H}_n\text{M}^{k+}$ .

<sup>b</sup>The adiabatic  $\Delta E_{ad}$  gives  $\Delta E$  (ZPE corrected) for the combined process  $\text{H}_n\text{M}^{k+} + e \rightarrow \text{H}_n\text{M}^{(k-1)+} \rightarrow \text{H} + \text{H}_{(n-1)}\text{M}^{(k-1)+}$ , in which  $\text{H}_{(n-1)}\text{M}^{(k-1)+}$  is produced at its optimal geometry.

spect to dissociation into  $\text{H}_n\text{X}^+ + \text{H}^+$ . All of these cations have local minima on their ground state potential energy surfaces with barriers that must be overcome to reach dissociation. The lifetimes of these multiply protonated species may be long enough to permit them to be experimentally observed.

(2) Because the above multiply protonated dications lie high above their respective dissociation products, and because the corresponding one-electron-reduced cations are geometrically unstable, a large amount of pent up energy can be released by adding a single electron (e.g., by charge transfer from a neighboring molecule or anion). These species thus may be good candidates for use in energy storage materials.

(3) The *triply charged*  $\text{H}_4\text{F}^{3+}$ ,  $\text{H}_3\text{Ne}^{3+}$ ,  $\text{H}_3\text{Ar}^{3+}$ , and *higher charged*  $\text{H}_4\text{Ne}^{4+}$ ,  $\text{H}_4\text{Ar}^{4+}$  cations as well as the  $\text{H}_2\text{Ne}^{2+}$  dication do not possess local minima on their ground state surfaces.  $\text{H}_4\text{Cl}^{3+}$  has a local minimum on its potential energy surface, but its zero-point corrected energy lies slightly above its dissociation barrier.

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